CAT 2017

Time: 180 Mins

Important Instructions

- (i) Total number of questions: 100
- (ii) Number of questions in Verbal Ability and Reading Comprehension (VARC): 34

SHIFT-1

- (iii) Number of questions in Data Interpretation and Logical Reasoning (DILR): 32
- (iv) Number of questions in Quantitative Ability (QA): 34
- (v) 60 minutes are allotted to attempt each section.
- (vi) 4 answer options for each MCQ type question.
- (vii) Answers are typed in the given space on the computer screen for Non-MCQ.
- (viii) For each correct answer: + 3 marks
- (ix) Negative marking (Applicable for wrong answers in MCQs): 1 mark

Verbal Ability and Reading Comprehension (VARC)

Passage 1

Directions (Q. 1 to 6): The passage below is accompanied by a set of six questions. Choose the best answer to each question.

Understanding where you are in the world is a basic survival skill, which is why we, like most species come hard-wired with specialised brain areas to create cognitive maps of our surroundings. Where humans are unique, though, with the possible exception of honeybees, is that we try to communicate this understanding of the world with others. We have a long history of doing this by drawing maps — the earliest versions yet discovered were scrawled on cave walls 14,000 years ago. Human cultures have been drawing them on stone tablets, papyrus, paper and now computer screens ever since.

Given such a long history of human map-making, it is perhaps surprising that it is only within the last few hundred years that north has been consistently considered to be at the top. In fact, for much of human history, north almost never appeared at the top, according to Jerry Brotton, a map historian... "North was rarely put at the top for the simple fact that north is where darkness comes from," he says. "West is also very unlikely to be put at the top because west is where the sun disappears."

Confusingly, early Chinese maps seem to buck this trend. But, Brotton, says, even though they did have compasses at the time, that isn't the reason that they placed north at the top. Early Chinese compasses were actually oriented to point south, which was considered to be more desirable than deepest darkest north. But in Chinese maps, the Emperor, who lived in the north of the country was always put at the top of the map, with everyone else, his loyal subjects, looking up towards him. "In Chinese culture the Emperor looks south because it's where the winds come from, it's a good direction. North is not very good but you are in a position of subjection to the emperor, so you look up to him," says Brotton.

Given that each culture has a very different idea of who, or what, they should look up to it's perhaps not surprising that there is very little consistency in the way early maps pointed. In ancient Egyptian times the top of the world was east, the position of sunrise. Early Islamic maps favoured south at the top because most of the early Muslim cultures were north of Mecca, so they imagined looking up (south) towards it. Christian maps from the same era (called Mappa Mundi) put east at the top, towards the Garden of Eden and with Jerusalem in the centre.

So, when did everyone get together and decide that north was the top? It's tempting to put it down to European explorers like Christopher Columbus and Ferdinand Megellan, who were navigating by the North Star. But Brotton argues that these early explorers didn't think of the world like that at all. "When Columbus describes the world it is in accordance with east being at the top, he says. "Columbus says he is going towards paradise, so his mentality is from a medieval Mappa Mundi. "We've got to remember, adds Brotton, that at the time, "no one knows what they are doing and where they are going."

- **Q.1.** Which one of the following best describes what the passage is trying to say?
 - **1.** It questions an explanation about how maps are designed.
- **2.** It corrects the misconception about the way maps are designed.
- **3.** It critiques a methodology used to create maps.
- **4.** It explores some myths about maps.

QUESTION PAPER

Total Marks: 300

- **Q. 2.** Early maps did NOT put north at the top for all the following reasons EXCEPT
 - 1. North was the source of darkness.
 - 2. South was favoured by some Emperors.
 - **3.** East and south were more important for religious reasons for some civilisations.
 - **4.** East was considered by some civilisations to be a more positive direction.
- **Q.3.** According to the passage, early Chinese maps placed north at the top because
 - **1.** the Chinese invented the compass and were aware of magnetic north.
 - 2. they wanted to show respect to the emperor.
 - **3.** the Chinese emperor appreciated the winds from the south.
 - **4.** north was considered the most desirable direction.
- **Q. 4.** It can be inferred from the passage that European explorers like Columbus and Megellan
 - 1. set the precedent for north-up maps
 - **2.** navigated by the compass

- **3.** used an eastward orientation for religious reasons
- **4.** navigated with the help of early maps
- **Q.5.** Which one of the following about the northern orientation of modern maps is asserted in the passage?
 - **1.** The biggest contributory factor was the understanding of magnetic north.
 - **2.** The biggest contributory factor was the role of European explorers.
 - **3.** The biggest contributory factor was the influence of Christian maps.
 - **4.** The biggest contributory factor is not stated in the passage.
- **Q. 6.** The role of natural phenomena in influencing map-making conventions is seen most clearly in
 - 1. early Egyptian maps
 - 2. early Islamic maps
 - 3. early Chinese maps
 - 4. early Christian maps

Passage 2

Directions (Q. 7 to 12): The passage below is accompanied by a set of six questions. Choose the best answer to each question.

I used a smartphone GPS to find my way through the cobblestoned maze of Geneva's Old Town, in search of a handmade machine that changed the world more than any other invention. Near a 13th-century cathedral in this Swiss city on the shores of a lovely lake, I found what I was looking for: a Gutenberg printing press. "This was the Internet of its day — at least as influential as the iphone," said Gabriel de Montmollin, the director of the Museum of the Reformation, toying with the replica of Johann Gutenberg's great invention.

Before the invention of the printing press, it used to take four monks up to a year to produce a single book. With the advance in movable type in 15th-century Europe, one press could crank out 3,000 pages a day. Before long, average people could travel to places that used to be unknown to them — with maps! Medical information passed more freely and quickly, diminishing the sway of quacks. The printing press offered the prospect that tyrants would never be able to kill a book or suppress an idea. Gutenberg's brainchild broke the monopoly that clerics had on scripture. And later, stirred by pamphlets from a version of that same press, the American colonies rose up against a king and gave birth to a nation.

So, a question in the summer of this 10th anniversary of the iPhone: has the device that is perhaps the most revolutionary of all time given us a single magnificent idea? Nearly every advancement of the written word through new technology has also advanced humankind. Sure, you can say the iPhone changed everything. By putting the world's recorded knowledge in the palm of a hand, it revolutionised work, dining, travel and socializing. It made us more narcissistic — here's more of me doing cool stuff! — and it unleashed an army of awful trolls. We no longer have the patience to sit through a baseball game without that reach to the pocket. And one more casualty of Apple selling more than a billion phones in a decade's time: daydreaming has become a lost art.

For all of that, I'm still waiting to see if the iPhone can do what the printing press did for religion and democracy... the Geneva museum makes a strong case that the printing press opened more minds than anything else...it's hard to imagine the French or American revolutions without those enlightened voices in print...

Not long after Steve Jobs introduced his iPhone, he said the bound book was probably headed for history's attic. Not so fast. After a period of rapid growth in e-books, something closer to the medium for Chaucer's volumes has made a great comeback.

The hope of the iphone, and the Internet in general, was that it would free people in closed societies. But the failure of the Arab Spring, and the continued suppression of ideas in North Korea, China and Iran, has not borne that out. The iphone is still young. It has certainly been "one of the most important, world-changing and successful products in history," as Apple C.E.O. Tim Cook said. But I'm not sure if the world changed for the better with the iphone — as it did with the printing press — or merely changed.

Q.7. The printing press has been likened to the Internet for which one of the following reasons?

- **1.** It enabled rapid access to new information and the sharing of new ideas.
- **2.** It represented new and revolutionary technology compared to the past.
- **3.** It encouraged reading among people by giving them access to thousands of books.
- **4.** It gave people access to pamphlets and literature in several languages.
- **Q. 8.** According to the passage, the invention of the printing press did all of the following EXCEPT
 - **1.** promoted the spread of enlightened political views across countries.
 - **2.** gave people direct access to authentic medical information and religious texts.
 - **3.** shortened the time taken to produce books and pamphlets.
 - **4.** enabled people to perform various tasks simultaneously.
- **Q. 9.** Steve Jobs predicted which one of the following with the introduction of the iphone?
 - **1.** People would switch from reading on the Internet to reading on their iphones.
 - **2.** People would lose interest in historical and traditional classics.
 - **3.** Reading printed books would become a thing of the past.
 - 4. The production of e-books would eventually fall.
- **Q. 10.** "I'm still waiting to see if the iPhone can do what the printing press did for religion and democracy." The author uses which one of the following to indicate his uncertainty?

- 1. The rise of religious groups in many parts of the world.
- **2.** The expansion in trolling and narcissism among users of the Internet.
- **3.** The continued suppression of free speech in closed societies.
- **4.** The decline in reading habits among those who use the device.
- **Q. 11.** The author attributes the French and American revolutions to the invention of the printing press because
 - **1.** maps enabled large numbers of Europeans to travel and settle in the American continent.
 - **2.** the rapid spread of information exposed people to new ideas on freedom and democracy.
 - **3.** it encouraged religious freedom among the people by destroying the monopoly of religious leaders on the scriptures.
 - **4.** it made available revolutionary strategies and opinions to the people.
- **Q. 12.** The main conclusion of the passage is that the new technology has
 - 1. some advantages, but these are outweighed by its disadvantages.
 - **2.** so far not proved as successful as the printing press in opening people's minds.
 - **3.** been disappointing because it has changed society too rapidly.
 - **4.** been more wasteful than the printing press because people spend more time daydreaming or surfing.

Passage 3

Directions (Q. 13 to 18): The passage below is accompanied by a set of six questions. Choose the best answer to each question.

This year alone, more than 8,600 stores could close, according to industry estimates, many of them the brandname anchor outlets that real estate developers once stumbled over themselves to court. Already there have been 5,300 retail closings this year... Sears Holdings — which owns K.mart — said in March that there's "substantial doubt" it can stay in business altogether and will close 300 stores this year. So far this year, nine national retail chains have filed for bankruptcy.

Local jobs are a major casualty of what analysts are calling, with only a hint of hyperbole, the retail apocalypse. Since 2002, department stores have lost 448,000 jobs, a 25% decline, while the number of store closures this year is on pace to surpass the worst depths of the Great Recession. The growth of online retailers, meanwhile, has failed to offset those losses, with the e-commerce sector adding just 178,000 jobs over the past 15 years. Some of those jobs can be found in the massive distribution centres, Amazon has opened across the country, often not too far from malls the company helped shutter.

But those are workplaces, not gathering places. The mall is both. And in the 61 years since the first enclosed one opened in suburban Minneapolis, the shopping mall has been where a huge swath of middle-class America went for far more than shopping. It was the home of first jobs and blind dates, the place for family photos and ear piercings, where goths and grandmothers could somehow walk through the same doors and find something they all liked. Sure, the food was lousy for you and the oceans of parking lots encouraged car- heavy development, something now scorned by contemporary planners. But for better or worse, the mall has been America's public square for the last 60 years.

So what happens when it disappears?

Think of your mall. Or think of the one you went to as a kid. Think of the perfume clouds in the department

stores. The fountains splashing below the skylights. The cinnamon wafting from the food court. As far back as ancient Greece, societies have congregated around a central marketplace. In medieval Europe, they were outside cathedrals. For half of the 20th century and almost 20 years into the new one, much of America has found their agora on the terrazzo between Orange Julius and Sbarro, Waldenbooks and the Gap, Sunglass Hut and Hot Topic. That mall was an ecosystem unto itself, a combination of community and commercialism peddling everything you needed and everything you didn't: Magic eye posters, Wind catchers, Air Jordans....

A growing number of Americans, however, don't see the need to go to any Macy's at all. Our digital lives are frictionless and ruthlessly efficient, with retail and romance available at a click. Malls were designed for leisure, abundance, ambling. You parked and planned to spend some time. Today, much of that time has been given over to busier lives and second jobs and apps that let you swipe right instead of haunt the food court. Malls, says Harvard business professor Leonard Schlesinger, "were built for patterns of social interaction that increasingly don't exist."

Q. 13. The central idea of this passage is that:

- **1.** the closure of malls has affected the economic and social life of middle-class America.
- **2.** the advantages of malls outweigh their disadvantages.
- **3.** malls used to perform a social function that has been lost.
- **4.** malls are closing down because people have found alternate ways to shop.
- **Q. 14.** Why does the author say in paragraph 2, 'the massive distribution centres Amazon has opened across the country, often not too far from malls the company helped shutter'?
 - **1.** To highlight the irony of the situation.
 - **2.** To indicate that malls and distribution centres are located in the same area.
 - **3.** To show that Amazon is helping certain brands go online.
 - **4.** To indicate that the shopping habits of the American middle class have changed.
- **Q. 15.** In paragraph 1, the phrase "real estate developers once stumbled over themselves to court" suggests that they
 - 1. took brand-name anchor outlets to court.
 - 2. no longer pursue brand-name anchor outlets.
 - **3.** collaborated with one another to get brandname anchor outlets.
 - **4.** were eager to get brand-name anchor outlets to set up shop in their mall.

- **Q. 16.** The author calls the mall an ecosystem into itself because
 - **1.** people of all ages and from all walks of life went there.
 - **2.** people could shop as well as eat in one place.
 - **3.** it was a commercial space as well as a gathering place.
 - **4.** it sold things that were needed as well as those that were not.
- **Q. 17.** Why does the author say that malls have been America's public square?
 - **1.** Malls did not bar anybody from entering the space.
 - **2.** Malls were a great place to shop for a huge section of the middle class.
 - **3.** Malls were a hangout place where families grew close to each other.
 - **4.** Malls were a great place for everyone to gather and interact.
- **Q. 18.** The author describes 'Perfume clouds in the department stores' in order to
 - **1.** evoke memories by painting a picture of malls.
 - 2. describe the smells and sights of malls.
 - **3.** emphasise that all brands were available under one roof.
 - **4.** show that malls smelt good because of the various stores and food court.

Passage 4

Directions (Q. 19 to 21): The passage below is accompanied by a set of three questions. Choose the best answer to each question.

Scientists have long recognised the incredible diversity within a species. But they thought it reflected evolutionary changes that unfolded imperceptibly, over millions of years. That divergence between populations within a species was enforced, according to Ernst Mayr, the great evolutionary biologist of the 1940s, when a population was separated from the rest of the species by a mountain range or a desert, preventing breeding across the divide over geologic scales of time. Without the separation, gene flow was relentless. But as the separation persisted, the isolated population grew apart and speciation occurred.

In the mid-1960s, the biologist Paul Ehrlich — author of The Population Bomb (1968) — and his Stanford University colleague Peter Raven challenged Mayr's ideas about speciation. They had studied checkerspot butterflies living in the Jasper Ridge Biological Preserve in California and it soon became clear that they were not examining a single population. Through years of capturing, marking and then recapturing the butterflies, they were able to prove that within the population, spread over just 50 acres of suitable checkerspot habitat, there were three

Among other ideas, Ehrlich and Raven argued in a new classic paper from 1969 that gene flow was not as predictable and ubiquitous as Mayr and his cohort maintained and thus evolutionary divergence between neighbouring groups in a population was probably common. They also asserted that isolation and gene flow were less important to evolutionary divergence than natural selection (when factors such as mate choice, weather, disease or predation cause better-adapted individuals to survive and pass on their successful genetic traits). For example, Ehrlich and Raven suggested that, without the force of natural selection, an isolated population would remain unchanged and that, in other scenarios, natural selection could be strong enough to overpower gene flow...

- **Q. 19.** Which of the following best sums up Ehrlich and Raven's argument in their classic 1969 paper?
 - **1.** Ernst Mayr was wrong in identifying physical separation as the cause of species diversity.
 - **2.** Checkerspot butterflies in the 50-acre Jasper Ridge Preserve formed three groups that rarely interacted with each other.
 - **3.** While a factor, isolation was not as important to speciation as natural selection.
 - **4.** Gene flow is less common and more erratic than Mayr and his colleagues claimed.

Q. 20. All of the following statements are true according to the passage EXCEPT

1. Gene flow contributes to evolutionary divergence.

- **2.** The population bomb questioned dominant ideas about species diversity.
- **3.** Evolutionary changes unfold imperceptibly over time.
- 4. Checkerspot butterflies are known to exhibit speciation while living in close proximity.
- **Q. 21.** The author discusses Mayr, Ehrlich and Raven to demonstrate that
 - **1.** evolution is a sensitive and controversial topic.
 - **2.** Ehrlich and Raven's ideas about evolutionary divergence are widely accepted by scientists.
 - **3.** the causes of speciation are debated by scientists.
 - **4.** checkerspot butterflies offer the best example of Ehrlich and Raven's ideas about speciation.

Passage 5

Directions (Q. 22 to 24): The passage below is accompanied by a set of three questions. Choose the best answer to each question.

Do sports mega events like the summer Olympic Games benefit the host city economically? It depends, but the prospects are less than rosy. The trick is converting several billion dollars in operating costs during the 17 – day fiesta of the Games into a basis for long-term economic returns. These days, the summer Olympic Games themselves generate total revenue of \$4 billion to \$5 billion, but the lion's share of this goes to the International Olympics Committee, the National Olympics Committees and the International Sports Federations. Any economic benefit would have to flow from the value of the Games as an advertisement for the city, the new transportation and communications infrastructure that was created for the Games, or the ongoing use of the new facilities.

Evidence suggests that the advertising effect is far from certain. The infrastructure benefit depends on the initial condition of the city and the effectiveness of the planning. The facilities benefit is dubious at best for buildings such as velodromes or natatoriums and problematic for 100,000-seat Olympic stadiums. The latter require a conversion plan for future use, the former are usually doomed to near vacancy. Hosting the summer Games generally requires 30-plus sports venues and dozens of training centers. Today, the Bird's Nest in Beijing sits virtually empty, while the Olympic Stadium in Sydney costs some \$30 million a year to operate.

Part of the problem is that Olympics planning takes place in a frenzied and time-pressured atmosphere of intense competition with the other prospective host cities — not optimal conditions for contemplating the future shape of an urban landscape. Another part of the problem is that urban land is generally scarce and growing scarcer. The new facilities often stand for decades or longer. Even if they have future use, are they the best use of precious urban real estate?

Further, cities must consider the human cost. Residential areas often are razed and citizens relocated (without adequate preparation or compensation). Life is made more hectic and congested. There are, after all, other productive uses that can be made of vanishing fiscal resources.

- **Q. 22.** The central point in the first paragraph is that the economic benefits of the Olympic Games
 - **1.** are shared equally among the three organising committees.
 - 2. accrue mostly through revenue from

advertisements and ticket sales.

- **3.** accrue to host cities, if at all, only in the long term.
- **4.** are usually eroded by expenditure incurred by the host city.

- **Q. 23.** Sports facilities built for the Olympics are not fully utilised after the Games are over because
 - **1.** their scale and the costs of operating them are large.
 - **2.** their location away from the city centre usually limits easy access.
 - **3.** the authorities do not adapt them to local conditions.
 - **4.** they become outdated being built with little planning and under time pressure.
- **Q. 24.** The author feels that the Games places a burden on the host city for all of the following reasons EXCEPT that
 - **1.** they divert scarce urban land from more productive uses.
 - **2.** they involve the demolition of residential structures to accommodate sports facilities and infrastructure.
 - **3.** the finances used to fund the Games could be better used for other purposes.
 - 4. the influx of visitors during the Games places a huge strain on the urban infrastructure.
- Q. 25. To me, a "classic" means precisely the opposite of what my predecessors understood: a work is classical by reason of its resistance to contemporaneity and supposed universality, by reason of its capacity to indicate human particularity and difference in that past epoch. The classic is not what tells me about shared humanity - or, more truthfully put, what let me recognise myself as already present in the past, what nourishes in me the illusion that everything has been like me and has existed only to prepare the way for me. Instead, the classic is what gives access to radically different forms of human consciousness for any given generation of readers and thereby expands the range of possibilities of what it means to be a human being.
 - **1.** A classic is able to focus on the contemporary human condition and a unified experience of human consciousness.
 - **2.** A classical work seeks to resist particularity and temporal difference even as it focuses on a common humanity.
 - **3.** A classic is a work exploring the new, going beyond the universal, the contemporary and the notion of a unified human consciousness.
 - **4.** A classic is a work that provides access to a universal experience of the human race as opposed to radically different forms of human consciousness.
- **Q. 26.** A translator of literary works needs a secure hold upon the two languages involved, supported by a good measure of familiarity

with the two cultures. For an Indian translating works in an Indian language into English, finding satisfactory equivalents in a generalised western culture of practices and symbols in the original would be less difficult than gaining fluent control of contemporary English. When a westerner works on texts in Indian languages the interpretation of cultural elements will be the major challenge, rather than control over the grammar and essential vocabulary of the language concerned. It is much easier to remedy lapses in language in a text translated into English, than flaws of content. Since it is easier for an Indian to learn the English language than it is for a Britishers or American to comprehend Indian culture, translations of Indian texts is better left to Indians.

- **1.** While translating, the Indian and the Westerner faces the same challenges but they have different skill profiles and the former has the advantage.
- **2.** As preserving cultural meanings is the essence of literary translation. Indians' knowledge of the local culture outweighs the initial disadvantage of lower fluency in English.
- **3.** Indian translators should translate Indian texts into English as their work is less likely to pose cultural problems which are harder to address than the quality of language.
- 4. Westerners might be good at gaining reasonable fluency in new languages, but as understanding the culture reflected in literature is crucial, Indians remain better placed.
- Q. 27. For each of the past three years, temperatures have hit peaks not seen since the birth of meteorology, and probably not for more than 110,000 years. The amount of carbon dioxide in the air is at its highest level in 4 million years. This does not cause storms like Harvey — there have always been storms and hurricanes along the Gulf of Mexico - but it makes them wetter and more powerful. As the seas warm, they evaporate more easily and provide energy to storm fronts. As the air above them warms, it holds more water vapour. For every half a degree Celsius in warming, there is about 3% increase in atmospheric moisture content. Scientists call this the Clausius-Clapeyron equation. This means the skies fill more quickly and have more to dump. The storm surge was greater because sea levels have risen 20 cm as a result of more than 100 years of human-related global warming which has melted glaciers and thermally expanded the volume of seawater.
 - **1.** The storm Harvey is one of the regular, annual ones from the Gulf of Mexico; global warming and Harvey are unrelated

phenomena.

- 2. Global warming does not breed storms but makes them more destructive; the Clausius-Clapeyron equation, though it predicts potential increase in atmospheric moisture content, cannot predict the scale of damage storms might wreck.
- **3.** Global warming melts glaciers, resulting in seawater volume expansion; this enables more water vapour to fill the air above faster. Thus, modern storms contain more destructive energy.
- **4.** It is naive to think that rising sea levels and the force of tropical storms are unrelated; Harvey was destructive, as global warming has armed it with more moisture content, but this may not be true of all storms.
- **Q. 28.** The five sentences labeled (1, 2, 3, 4, 5) given in this question, when properly sequenced, form a coherent paragraph. Each sentence is labelled with a number. Decide on the proper order for the sentences and key in this sequence of five numbers as your answer.
 - 1. The process of handing down implies not a passive transfer, but some contestation in defining what exactly is to be handed down.
 - 2. Wherever Western scholars have worked on the Indian past, the selection is even more apparent and the inventing of a tradition much more recognisable.
 - **3.** Every generation selects what it requires from the past and makes its innovations, some more than others.
 - **4.** It is now a truism to say that traditions are not handed down unchanged, but are invented.
 - **5.** Just as life has death as its opposite, so is tradition by default the opposite of innovation.
- **Q. 29.** The five sentences labelled (1, 2, 3, 4, 5) given in this question, when properly sequenced, form a coherent paragraph. Each sentence is labelled with a number. Decide on the proper order for the sentences and key in this sequence of five numbers as your answer.
 - 1. Scientists have for the first time managed to edit genes in a human embryo to repair a genetic mutation, fuelling hopes that such procedures may one day be available outside laboratory conditions.
 - **2.** The cardiac disease causes sudden death in otherwise healthy young athletes and affects about one in 500 people overall.
 - **3.** Correcting the mutation in the gene would not only ensure that the child is healthy but also prevents transmission of the mutation to future generations.
 - 4. It is caused by a mutation in a particular

gene and a child will suffer from the condition even if it inherits only one copy of the mutated gene.

- **5.** In results announced in Nature this week, scientists fixed a mutation that thickens the heart muscle, a condition called hypertrophic cardiomyopathy.
- **Q. 30.** The five sentences labelled (1, 2, 3, 4, 5) given in this question, when properly sequenced, form a coherent paragraph. Each sentence is labelled with a number. Decide on the proper order for the sentences and key in this sequence of five numbers as your answer.
 - 1. The study suggests that the disease did not spread with such intensity, but that it may have driven human migrations across Europe and Asia.
 - **2.** The oldest sample came from an individual who lived in southeast Russia about 5,000 years ago.
 - **3.** The ages of the skeletons correspond to a time of mass exodus from today's Russia and Ukraine into western Europe and Central Asia, suggesting that a pandemic could have driven these migrations.
 - **4.** In the analysis of fragments of DNA from 101 Bronze Age skeletons for sequences from *Yersinia pestis*, the bacterium that causes the disease, seven tested positive.
 - **5.** DNA from Bronze Age human skeletons indicate that the black plague could have emerged as early as 3,000 BCE, long before the epidemic that swept through Europe in the mid-1300s.
- **Q. 31.** The five sentences labelled (1, 2, 3, 4, 5) given in this question, when properly sequenced, form a coherent paragraph. Each sentence is labelled with a number. Decide on the proper order for the sentences and key in this sequence of five numbers as your answer.
 - 1. This visual turn in social media has merely accentuated this announcing instinct of ours, enabling us with easy-to-create, easy-to-share, easy-to-store and easy-to-consume platforms, gadgets and apps.
 - 2. There is absolutely nothing new about us framing the vision of who we are or what we want, visually or otherwise, in our Facebook page, for example.
 - **3.** Turning the pages of most family albums, which belong to a period well before the digital dissemination of self-created and self-curated moments and images, would reconfirm the basic instinct of documenting our presence in a particular space, on a significant occasion, with others who matter.
 - 4. We are empowered to book our faces and

act as celebrities within the confinement of our respective friend lists and communicate our activities, companionship and locations with minimal clicks and touches.

- **5.** What is unprecedented is not the desire to put out newsfeeds related to the self, but the ease with which this broadcast operation can now be executed, often provoking (un) anticipated responses from beyond one's immediate location.
- **Q. 32.** Five sentences related to a topic are given below. Four of them can be put together to form a meaningful and coherent short paragraph. Identify the odd one out. Choose its number as your answer and key it in.
 - **1.** People who study children's language spend a lot of time watching how babies react to the speech they hear around them.
 - 2. They make films of adults and babies interacting and examine them very carefully to see whether the babies show any signs of understanding what the adults say.
 - **3.** They believe that babies begin to react to language from the very moment they are born.
 - 4. Sometimes the signs are very subtle slight movements of the baby's eyes or the head or the hands.
 - **5.** You'd never notice them if you were just sitting with the child, but by watching a recording over and over, you can spot them.
- **Q. 33.** Five sentences related to a topic are given below. Four of them can be put together to form a meaningful and coherent short paragraph. Identify the odd one out. Choose its number as your answer and key it in.
 - 1. Neuroscientists have just begun studying exercise's impact within brain cells on the genes themselves.
 - **2.** Even there, in the roots of our biology, they' ve found signs of the body's influence on

the mind.

- **3.** It turns out that moving our muscles produces proteins that travel through the bloodstream and into the brain, where they play pivotal roles in the mechanisms of our highest thought processes.
- 4. In today's technology-driven, plasmascreened-in world, it's easy to forget that we are born movers-animals, in fact — because we've engineered movement right out of our lives.
- **5.** It's only in the past few years that neuroscientists have begun to describe these factors and how they work, and each new discovery adds awe-inspiring depth to the picture.
- **Q. 34.** Five sentences related to a topic are given below. Four of them can be put together to form a meaningful and coherent short paragraph. Identify the odd one out. Choose its number as your answer and key it in.
 - **1.** The water that made up ancient lakes and perhaps an ocean was lost.
 - **2.** Particles from the sun collided with molecules in the atmosphere, knocking them into space or giving them an electric charge that caused them to be swept away by the solar wind.
 - **3.** Most of the planet's remaining water is now frozen or buried, but clues over the past decade suggested that some liquid water, a presumed necessity for life, might survive in underground aquifers.
 - **4.** Data from NASA's MAVEN orbiter show that solar storms stripped away most of Mars's once-thick atmosphere.
 - **5.** A recent study reveals how Mars lost much of its early water, while another indicates that some liquid water remains.

Data Interpretation and Logical Reasoning (DILR)

Directions (Q. 1 to 4): Answer the questions on the basis of following information.

Healthy bites is a fastfood joint serving three items, burgers, fries and ice cream. It has two employees Anish and Bani who prepare the items ordered by the clients. Preparation time is 10 minutes for a burger and 2 minutes for an order of Ice cream. An employee can prepare only one of these items at a time. The fries are prepared in an automatic fryer which can prepare upto to 3 portions of fries at a time, and takes 5 minutes irrespective of the number of portions. The fryer does not need an employee to constantly attend to it, and we can ignore the time taken by an employee to start and stop the fryer; thus, an employee can be engaged in preparing other items while the frying is on. However, fries cannot be prepared in anticipation of future orders.

Healthy bites wishes to serve the orders as early as possible. The individual items in any order are served as and when ready; however, the order is considered to be completely served only when all the items of that order are served.

The table below gives the orders of three clients and the times at which they placed their orders:

Client no.	Time	Order		
1	10:00 a.m.	1 burger, 3 portions of fries, 1 order of ice cream		
2	10:05 a.m.	2 portions of fries, 1 order of ice cream		
3	10:07 a.m.	1 burger, 1 portion of fries		

Q.1. Assume that only one client's order can be **Q.3.** Suppose the employees are allowed to process processed at any given point of time. So, Anish multiple orders at a time, but the preference or Bani cannot start preparing a new order while a previous order is being prepared. At what time is the order placed by Client 1 completely served? 1. 10:10 1. 10:17 **2.** 10:10 **3.** 10:15 **4.** 10:20 Q.2. Assume that only one client's order can be processed at any given point of time. So, Anish or Bani cannot start preparing a new order

while a previous order is being prepared. At what time is the order placed by Client 3 completely served?

- 1. 10:35 **2.** 10:22 **3.** 10:25 **4.** 10:17
- would be to finish orders of clients who placed their orders earlier. At what time was the order placed by Client 2 completely served? **2.** 10:12 **3.** 10:15 **4.** 10:17 Q. 4. Suppose the employees are allowed to process multiple orders at a time, but the preference would be to finish orders of clients who placed their orders earlier. Also assume that the fourth client came in only

at 10:35. Between 10:00 and 10:30, for how many minutes is exactly one of the employees idle? **2.** 10 1. 7 3. 15 4. 23

Directions (Q. 5 to 8): Answer the questions on the basis of following information.

A study to look at the early learning of rural kids was carried out in a number of villages spanning three states, chosen from the North-East (NE), the West (W) and the South (S). 50 four-year old kids each were sampled from each of the 150 villages from NE, 250 villages from W and 200 villages from S. It was found that of the 30000 surveyed kids 55% studied in primary schools run by the government (G), 37% in private schools (P) while the remaining 8% did not go to school (O).

The kids surveyed were further divided into two groups based on whether their mothers dropped out of school before completing primary education or not. The table below gives the number of kids in different types of schools for mothers who dropped out of school before completing primary education:

	G	Р	0	Total
NE	4200	500	300	5000
W	4200	1900	1200	7300
S	5100	300	300	5700
TOTAL	13500	2700	1800	18000

It is also known that:

- 1. In S, 60% of the surveyed kids were in G. Moreover, in S, all surveyed kids whose mothers had completed primary education were in school.
- 2. In NE, among the O kids, 50% had mothers who had dropped out before completing primary education.
- 3. The number of kids in G in NE was the same as the number of kids in G in W.
- **Q.5.** What percentage of kids from S were studying in P?

1. 37% 2. 6% 3. 79% 4. 56%

Q.6. Among the kids in W whose mothers had completed primary education, how many were not in school?

1. 300 **2.** 1200 3. 1050 4. 1500

Q. 7. In a follow up survey of the same kids two years later, it was found that all the kids were now in school. Of the kids who were not in school earlier, in one region, 25% were in G now, whereas the rest were enrolled in P; in the second region, all such kids were in G now; while in the third region, 50% of such kids had now joined G while the rest had joined P. As a result, all the three regions were put together,

50% of the kids who were earlier out of school had joined G. It was also seen that no surveyed kid had changed schools.

What number of the surveyed kids now were in G in W?

1. 6000 **2.** 5250 **3.** 6750 4. 6300

Q. 8. In a follow up survey of the same kids two years later, it was found that all the kids were now in school. Of the kids who were not in school earlier, in one region, 25% were in G now, whereas the rest were enrolled in P; in the second region, all such kids were in G now; while in the third region, 50% of such kids had now joined G while the rest had joined P. As a result, in all three regions put together, 50% of the kids who were earlier out of school had

joined G. It was also seen that no surveyed kid had changed schools.

What percentage of the surveyed kids in S, whose mothers had dropped out before completing primary education, were in G now?

1. 94.7% **2.** 89.5%

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3. 93.4%
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4. Cannot be determined from the given information

Directions (Q. 9 to 12): *Answer the questions on the basis of following information.*

Applicants for the doctoral programmes of Ambi Institute of Engineering (AIE) and Bambi Institute of Engineering (BIE) have to appear for a Common Entrance Test (CET). The test has three sections: Physics (P), Chemistry (C), and Maths (M). Among those appearing for CET, those at or above the 80th percentile in at least two sections, and at or above the 90th percentile overall, are selected for Advanced Entrance Test (AET) conducted by AIE. AET is used by AIE for final selection.

For the 200 candidates who are at or above the 90th percentile overall based on CET, the following are known about their performance in CET:

1. No one is below the 80th percentile in all 3 sections.

- 2. 150 are at or above the 80^{th} percentile in exactly two sections.
- 3. The number of candidates at or above the 80th percentile only in P is the same as the number of candidates at or above the 80th percentile only in C. The same is the number of candidates at or above the 80th percentile only in M.
- 4. Number of candidates below 80^{th} percentile in P : Number of candidates below 80^{th} percentile in C : Number of candidates below 80^{th} percentile in M = 4 : 2 : 1.

BIE uses a different process for selection. If any candidate is appearing in the AET by AIE, BIE considers their AET score for final selection provided the candidate is at or above the 80th percentile in P. Any other candidate at or above the 80th percentile in P in CET, but who is not eligible for the AET, is required to appear in a separate test to be conducted by BIE for being considered for final selection. Altogether, there are 400 candidates this year who are at or above the 80th percentile in P.

Q. 9. What best can be concluded about the number of candidates sitting for the separate test for BIE who were at or above the 90th percentile overall in CET?

1. 3 or 10 **2.** 10 **3.** 5 **4.** 7 or 10

- **Q. 10.** If the number of candidates who are at or above the 90th percentile overall and also at or above the 80th percentile in all the three sections in CET is actually a multiple of 5, what is the number of candidates who are at or above the 90th percentile overall and at or above the 80th percentile in both P and M in CET?
- **Q. 11.** If the number of candidates who are at or above the 90th percentile overall and also at or above the 80th percentile in all three sections in CET is actually a multiple of 5, then how many candidates were shortlisted for the AET for AIE?
- **Q. 12.** If the number of candidates who are at or above the 90th percentile overall and also are at or above the 80th percentile in P in CET, is more than 100, how many candidates had to sit for the separate test for BIE?

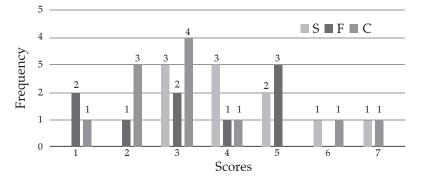
1. 299 **2.** 310 **3.** 321 **4.** 330

Directions (Q. 13 to 16): Answer the questions on the basis of following information.

Simple Happiness Index (SHI) of a country is computed on the basis of three, parameters: social support (S), freedom to life choices (F) and corruption perception (C). Each of these three parameters is measured on a scale of 0 to 8 (integers only). A country is then categorised based on the total score obtained by summing the scores of all the three parameters, as shown in the following table:

Total Score	0–4	5–8	9–13	14–19	20–24
Category	Very unhappy	Unhappy	Neutral	Нарру	Very happy

Following diagram depicts the frequency distribution of the scores in S, F and C of 10 countries – Amda, Benga, Calla, Delma, Eppa, Varsa, Wanna, Xanda, Yanga and Zooma:



Further, the following are known.

- 1. Amda and Calla jointly have the lowest total score, 7, with identical scores in all the three parameters.
- 2. Zooma has a total score of 17.
- 3. All the 3 countries, which are categorised as happy, have the highest score in exactly one parameter.

Q. 13. What is Amda's score in F?	1. 14	2. 15	3. 16	4. 17	
Q. 14. What is Zooma's score in S?	Q. 16. If Benga se				
Q. 15. Benga and Delma, two countries categorised as	what is the maximum number of countries with				
happy, are tied with the same total score. What	a score of 1	3?			
is the maximum score they can have?	1. 0	2. 1	3. 2	4. 3	

Directions (Q. 17 to 20): Answer the questions on the basis of following information.

There are 21 employees working in a division, out of whom 10 are special-skilled employees (SE) and the remaining are regular-skilled employees (RE). During the next five months, the division has to complete five projects every month. Out of the 25 projects, 5 projects are "challenging", while the remaining ones are "standard". Each of the challenging projects has to be completed in different months. Every month, five teams— T_1 , T_2 , T_3 , T_4 and T_5 , work on one project each. T_1 , T_2 , T_3 , T_4 and T_5 are allotted the challenging project in the first, second, third, fourth and fifth month, respectively. The team assigned the challenging project has one more employee than the rest.

In the first month, T_1 has one more SE than T_2 , T_2 has one more SE than T_3 , T_3 has one more SE than T_4 , and T_4 has one more SE than T_5 . Between two successive months, the composition of the teams changes as follows:

- (a) The team allotted the challenging project, gets two SE from the team which was allotted the challenging project in the previous month. In exchange, one RE is shifted from the former team to the latter team.
- (b) After the above exchange, if T_1 has any SE and T_5 has any RE, then one SE is shifted from T_1 to T_5 , and one RE is shifted from T_5 to T_1 . Also, if T_2 has any SE and T_4 has any RE, then one SE is shifted from T_2 to T_4 , and one RE is shifted from T_4 to T_2 .

Each standard project has a total of 100 credit points, while each challenging project has 200 credit points. The credit points are equally shared between the employees included in that team.

Q. 17. The number of times in which the composition of team T_2 and the number of times in which composition of team T_4 remained unchanged in two successive months are:

1. (2, 1) **2.** (1, 0) **3.** (0, 0) **4.** (1, 1)

- **Q. 18.** The number of SE in T_1 and T_5 for the projects in the third month are, respectively:
 - **1.** (0, 2) **2.** (0, 3) **3.** (1, 2) **4.** (1, 3)
- **Q. 19.** Which of the following CANNOT be the total

credit points earned by any employee from the projects?

- **1.** 140 **2.** 150 **3.** 170 **4.** 200
- **Q. 20.** One of the employees named Aneek scored 185 points. Which of the following CANNOT be true?
 - **1.** Aneek worked only in teams $T_{1'}$, $T_{2'}$, $T_{3'}$ and T_4 .
 - **2.** Aneek worked only in teams T_1 , T_2 , T_4 , and T_5 .
 - 3. Aneek worked only in teams $T_{2'} T_{3'} T_{4'}$ and T_5 .
 - 4. Aneek worked only in teams T_1 , T_3 , T_4 , and T_5 .

Directions (Q. 21 to 24): Answer the questions on the basis of following information.

In a square layout of site 5 m \sim 5 m 25 equal-sized square platforms of different heights are built. The heights (in metre) of individual platforms are as shown below:

6	1	2	4	3
9	5	3	2	8
7	8	4	6	5
3	9	5	1	2
1	7	6	3	9

Individuals (all of same height) are seated on these platforms. We say an individual A can reach individual B, if all the three following conditions are met;

- (a) A and B are in the same row or column
- (b) A is at a lower height than B

(c) If there is/are any individual(s) between A and B, such individual(s) must be at a height lower than that of A.

Thus in the table given above, consider the Individual seated at height 8 on 3^{rd} row and 2^{nd} column. He can be reached by four individuals. He can be reached by the individual on his left at height 7, by the two individuals on his right at heights of 4 and 6 and by the individual above at height 5.

Rows in the layout are numbered from top to bottom and columns are numbered from left to right.

Q. 21. How many individuals in this layout can be reached by just one individual?

1. 3 **2.** 5 **3.** 7 **4.** 8

- **Q. 22.** Which of the following is true for any individual at a platform of height 1 m in this layout?
 - **1.** They can be reached by all the individuals in their own row and column.
 - 2. They can be reached by at least 4 individuals.
 - **3.** They can be reached by at least one individual.
 - 4. They cannot be reached by anyone.
- **Q. 23.** We can find two individuals who cannot be reached by anyone in
 - **1.** the last row.

- **2.** the fourth row.
- 3. the fourth column.
- **4.** the middle column.
- **Q. 24.** Which of the following statements is true about this layout?
 - **1.** Each row has an individual who can be reached by 5 or more individuals.
 - **2.** Each row has an individual who cannot be reached by anyone.
 - **3.** Each row has at least two individuals who can be reached by an equal number of individuals.
 - **4.** All individuals at the height of 9 m can be reached by at least 5 individuals.

Directions (Q. 25 to 28): Answer the questions on the basis of following information.

A new airlines company is planning to start operations in a country. The company has identified ten different cities which they plan to connect through their network to start with. The flight duration between any pair of cities will be less than one hour. To start operations, the company has to decide on a daily schedule.

The underlying principle that they are working on is the following:

Any person staying in any of these 10 cities should be able to make a trip to any other city in the morning and should be able to return by the evening of the same day.

- Q. 25. If the underlying principle is to be satisfied in such a way that the journey between any two cities can be performed using only direct (nonstop) flights, then the minimum number of direct flights to be scheduled is:
 1. 45
 2. 90
 3. 180
 4. 135
- **Q. 26.** Suppose three of the ten cities are to be developed as hubs. A hub is a city which is connected with every other city by direct flights each way, both in the morning as well as in the evening. The only direct flights which will be scheduled are originating and/or terminating in one of the hubs. Then the minimum number of direct flights that need to be scheduled so that the underlying principle of the airline to serve all the ten cities is met without visiting more than one hub during one trip is:

1. 54 **2.** 120 **3.** 96 **4.** 60

- **Q. 27.** Suppose the 10 cities are divided into 4 distinct groups G1, G2, G3, G4 having 3, 3, 2 and 2 cities respectively and that G1 consists of cities named A, B and C. Further, suppose that direct flights are allowed only between two cities satisfying one of the following:
 - **1.** Both cities are in G1
 - 2. Between A and any city in G2

- 3. Between B and any city in G3
- 4. Between C and any city in G4

Then the minimum number of direct flights that satisfies the underlying principle of the airline is:

- **Q. 28.** Suppose the 10 cities are divided into 4 distinct groups Gl, G2, G3, G4 having 3, 3, 2 and 2 cities respectively and that Gl consists of cities named A, B and C. Further, suppose that direct flights are allowed only between two cities satisfying one of the following:
 - 1. Both cities are in G1
 - 2. Between A and any city in G2
 - 3. Between B and any city in G3
 - 4. Between C and any city in G4

However, due to operational difficulties at A, it was later decided that the only flights that would operate at A would be those to and from B. Cities in G2 would have to be assigned to G3 or to G4.

What would be the maximum reduction in the number of direct flights as compared to the situation before the operational difficulties arose?

Directions (Q. 29 to 32): Answer the questions on the basis of following information.

Four cars need to travel from Akala (A) to Bakala (B). Two routes are available, one via Mamur (M) and the other via Nanur (N). The roads from A to M, and from N to B, are both short and narrow. In each case, one car takes 6 minutes to cover the distance, and each additional car increases the travel time per car by 3 minutes because of congestion. (For example, if only two cars drive from A to M, each car takes 9 minutes.) On the road from A to N, one car takes 20 minutes, and each additional car increases the travel time per car by 1 minute. On the road from M to B, one car takes 20 minutes, and each additional car increases the travel time per car by 0.9 minute.

The police department orders each car to take a particular route in such a manner that it is not possible for any car to reduce its travel time by not following the order, while the other cars are following the order.

- **Q. 29.** How many cars would be asked to take the route A-N-B, that is Akala-Nanur-Bakala route, by the police department?
- **Q. 30.** If all the cars follow the police order, what is the difference in travel time (in minutes) between a car which takes the route A-N-B and a car that takes the route A-M-B?

1. 1 **2.** 0.1 **3.** 0.2 **4.** 0.9

Q. 31. A new one-way road is built from M to N. Each car now has three possible routes to travel from A to B: A-M-B, A-N-B and A-M-N-B. On the road from M to N, one car takes 7 minutes and each additional car increases the travel time per car by 1 minute. Assume that any car taking the A-M-N-B route travels the A-M portion at the same time as other cars taking the A-M-B route, and the N-B portion at the same time as other cars taking the A-N-B route.

How many cars would the police department order to take the A-M-N-B route so that it

Quantitative Aptitude (QA)

- **Q.1.** Arun's present age in years is 40% of Barun's. In another few years, Arun's age will be half of Barun's. By what percentage will Barun's age increase during this period?
- **Q. 2.** A person can complete a job in 120 days. He works alone on Day 1. On Day 2, he is joined by another person who also can complete the job in exactly 120 days. On Day 3, they are joined by another person of equal efficiency. Like this, everyday a new person with the same efficiency joins the work. How many days are required to complete the job?
- **Q.3.** An elevator has a weight limit of 630 kg. It is carrying a group of people of whom the heaviest weighs 57 kg and the lightest weighs 53 kg. What is the maximum possible number of people in the group?
- **Q. 4.** A man leaves his home and walks at a speed of 12 km per hour, reaching the railway station 10 minutes after the train had departed. If instead he had walked at a speed of 15 km per hour, he would have reached the station 10 minutes before the train's departure. The distance (in km) from his home to the railway station is?
- Q. 5. Ravi invests 50% of his monthly savings in fixed deposits. 30% of the rest of his savings is invested in stocks and the rest goes into Ravi's savings bank account. If the total amount deposited by him in the bank (for savings account and fixed deposits) is ₹59500, then Ravi's total monthly savings (in ₹) is
- **Q. 6.** If a seller gives a discount of 15% on retail price, she still makes a profit of 2%. Which of

is not possible for any car to reduce its travel time by not following the order while the other cars follow the order? (Assume that the police department would never order all the cars to take the same route.)

Q. 32. A new one-way road is built from M to N. Each car now has three possible routes to travel from A to B: A-M-B, A-N-B and A-M-N-B. On the road from M to N, one car takes 7 minutes and each additional car increases the travel time per car by 1 minute. Assume that any car taking the A-M-N-B route travels the A-M portion at the same time as other cars taking the A-M-B route, and the N-B portion at the same time as other cars taking the A-N-B route.

If all the cars follow the police order, what is the minimum travel time (in minutes) from A to B? (Assume that the police department would never order all the cars to take the same route.)

1.	26	2. 32	3. 29.9	4. 30

the following ensures that she makes a profit of 20%?

- 1. Give a discount of 5% on retail price.
- 2. Give a discount of 2% on retail price.
- 3. Increase the retail price by 2%.
- **4.** Sell at retail price.
- **Q.7.** A man travels by a motor boat down a river to his office and back. With the speed of the river unchanged, if he doubles the speed of his motor boat, then his total travel time gets reduced by 75%. The ratio of the original speed of the motor boat to the speed of the river is
 - **1.** $\sqrt{6}:\sqrt{2}$ **2.** $\sqrt{7}:2$
 - **3.** $2\sqrt{5}:3$ **4.** 3:2
- Q. 8. Suppose, C1, C2, C3, C4, and C5 are five companies. The profits made by Cl, C2, and C3 are in the ratio 9 : 10 : 8 while the profits made by C2, C4, and C5 are in the ratio of 18 : 19 : 20. If C5 has made a profit of ₹19 crore more than C1, then the total profit (in ₹) made by all five companies is

- **3.** 348 crore **4.** 345 crore
- **Q.9.** The number of girls appearing for an admission test is twice the number of boys. If 30% of the girls and 45% of the boys get admission, the percentage of candidates who do not get admission is
 - **1.** 35 **2.** 50 **3.** 60 **4.** 65
- **Q. 10.** A stall sells popcorn and chips in packets of three sizes: large, super and jumbo. The number of large, super and jumbo packets in its stock are in the ratio 7 : 17 : 16 for popcorn and 6 : 15 : 14 for chips. If the total number of popcorn packets in its stock is the same as that

of chips packets, then the numbers of jumbo popcorn packets and jumbo chips packets are in the ratio:

1. 1:1 **2.** 8:7 **3.** 4:3 **4.** 6:5

Q. 11. In a market, the price of medium quality mangoes is half that of good mangoes. A shopkeeper buys 80 kg good mangoes and 40 kg medium quality mangoes from the market and then sells all these at a common price which is 10% less than the price at which he bought the good ones. His overall profit is

1. 6% **2.** 8% **3.** 10% **4.** 12%

Q. 12. If Fatima sells 60 identical toys at a 40% discount on the printed price, then she makes 20% profit. Ten of these toys are destroyed in fire. While selling the rest, how much discount should be given on the printed price so that she can make the same amount of profit?

Q. 13. If *a* and *b* are integers of opposite signs such that $(a + 3)^2 : b^2 = 9 : 1$ and

 $(a-1)^2:(b-1)^2=4:1,$

then the ratio $a^2 : b^2$ is:

1.

1

1. 9:4 **2.** 81:4 **3.** 1:4 **4.** 25:4

Q. 14. A class consists of 20 boys and 30 girls. In the mid-semester examination, the average score of the girls was 5 higher than that of the boys. In the final exam, however, the average score of the girls dropped by 3 while the average score of the entire class increased by 2. The increase in the average score of the boys is:

Q. 15. The area of the closed region bounded by the equation |x| + |y| = 2 in the two-dimensional plane is:

1. 4π **2.** 4 **3.** 8 **4.** 2π

Q. 16. From a triangle ABC with sides of lengths 40 ft, 25 ft and 35 ft, a triangular portion GBC is cut off where G is the centroid of ABC. The area, in sq ft, of the remaining portion of triangle ABC is:

1.
$$225\sqrt{3}$$
 2. $\frac{500}{\sqrt{3}}$ **3.** $\frac{275}{\sqrt{3}}$ **4.** $\frac{250}{\sqrt{3}}$

Q. 17. Let ABC be a right-angled isosceles triangle with hypotenuse BC. Let BQC be a semi-circle, away from A, with diameter BC. Let BPC be an arc of a circle centered at A and lying between BC and BQC. If AB has length 6 cm then the area, in sq cm, of the region enclosed by BPC and BQC is:

$$.9\pi - 18$$
 2. 18 **3.** 9π **4.** 9

- **Q. 18.** A solid metallic cube is melted to form five solid cubes whose volumes are in the ratio 1 : 1 : 8 : 27 : 27. The percentage by which the sum of the surface areas of these five cubes exceeds the surface area of the original cube is nearest to:
 - **1.** 10 **2.** 50 **3.** 60 **4.** 20

- **Q. 19.** A ball of diameter 4 cm is kept on top of a hollow cylinder standing vertically. The height of the cylinder is 3 cm, while its volume is 9π cubic centimeters. Then the vertical distance, in cm, of the topmost point of the ball from the base of the cylinder is:
- **Q. 20.** Let ABC be a right-angled triangle with BC as the hypotenuse. Lengths of AB and AC are 15 km and 20 km, respectively. The minimum possible time, in minutes, required to reach the hypotenuse from A at a speed of 30 km per hour is:
- **Q. 21.** Suppose, $\log_3 x = \log_{12} y = a$, where *x*, *y* are positive numbers. If *G* is the geometric mean of *x* and *y*, and $\log_6 G$ is equal to:

1.
$$\sqrt{a}$$
 2. $2a$ 3. $a/2$ 4. a
Q. 22. If $x + 1 = x^2$ and $x > 0$, then $2x^4$ is;
1. $6 + 4\sqrt{5}$ 2. $3 + 3\sqrt{5}$
3. $5 + 3\sqrt{5}$ 4. $7 + 3\sqrt{5}$

Q. 23. The value of $\log_{0.008} \sqrt{5} + \log_{\sqrt{3}} 81 - 7$ is equal to:

1.
$$\frac{1}{3}$$
 2. $\frac{2}{3}$ 3. $\frac{5}{6}$ 4. $\frac{7}{6}$

Q. 24. If $9^{x-\frac{1}{2}} - 2^{2x-2} = 4^x - 3^{2x-3}$, then *x* is:

1.
$$\frac{3}{2}$$
 2. $\frac{2}{5}$ 3. $\frac{3}{4}$ 4. $\frac{4}{9}$

- **Q. 25.** The number of solutions (x, y, z) to the equation x y z = 25, where x, y and z are positive integers such that $x \le 40$, $y \le 12$ and $z \le 12$ is: **1.** 101 **2.** 99 **3.** 87 **4.** 105
- **Q. 26.** For how many integers *n*, will the inequality $(n-5)(n-10) 3(n-2) \le 0$ be satisfied?
- **Q. 27.** If $f_1(x) = x^2 + 11x + n$ and $f_2(x) = x$, then the largest positive integer *n* for which the equation $f_1(x) = f_2(x)$ has two distinct real roots is:
- **Q. 28.** If *a*, *b*, *c*, and are integers such that a + b + c + d = 30then the minimum possible value of $(a - b)^2 + (a - c)^2 + (a - d)^2$ is:
- **Q. 29.** Let AB, CD, EF, GH, and JK be five diameters of a circle with center at O. In how many ways can three points be chosen out of A, B, C, D, E, F, G, H, J, K, and Q so as to form a triangle?
- **Q. 30.** The shortest distance of the point $\left(\frac{1}{2}, 1\right)$ from the curve y = |x 1| + |x + 1| is

1. 1 **2.** 0 **3.**
$$\sqrt{2}$$
 4. $\sqrt{\frac{3}{2}}$

Q. 31. If the square of the 7th term of an arithmetic progression with positive common difference equals the product of the 3rd and 17th terms, then the ratio of the first term to the common difference is:

1. 2:3 **2.** 3:2 **3.** 3:4 **4.** 4:3

Q. 32. In how many ways can 7 identical erasers be distributed among 4 kids in such a way that each kid gets at least one eraser but nobody gets more than 3 eraser?

Q. 33.
$$f(x) = \frac{5x+2}{3x-5}$$
 and $g(x) = x^2 - 2x - 1$, then the

value of *g*(*f*(*f*(3))) is:

1. 2 2.
$$\frac{1}{3}$$
 3. 6 4. $\frac{2}{3}$

Q. 34. Let a_1, a_2, \dots, a_n be an arithmetic progression with $a_1 = 3$ and $a_2 = 7$. If $a_1 + a_2 + \dots + a_n = 1830$, then what is the smallest positive integer *m* such that $m(a_1 + a_2 + \dots + a_n) > 1830$? **1.** 8 **2.** 9 **3.** 10 **4.** 11

Answer Key

Verbal Ability and Reading Comprehension (VARC)

1. (2)	2. (2)	3. (2)	4. (3)	5. (4)	6. (1)	7. (1)	8. (4)	9. (3)	10. (3)
11. (2)	12. (2)	13. (3)	14. (1)	15. (2)	16. (3)	17. (4)	18. (1)	19. (3)	20. (2)
21. (3)	22. (3)	23. (1)	24. (4)	25. (3)	26. (3)	27. (3)	28. 54132	29. 15243	30. 54123
31. 32145	32. 3	33.4	34. 1						

Data Interpretation and Logical Reasoning (DILR)

1. (2)	2. (3)	3. (1)	4. (2)	5. (1)	6. (1)	7. (1)	8. (1)	9. (1)	10. 60
11. 170	12. (1)	13. 1	14. 6	15. (2)	16. (2)	17. (2)	18. (1)	19. (2)	20. (4)
21. (3)	22. (4)	23. (3)	24. (3)	25. (3)	26. (3)	27. 40	28. 4	29. 2	30. (2)
31.2	32. (2)								

Quantitative Aptitude (QA)

1. 20	2. 15	3. 11	4.20	5.70000	6. (4)	7. (2)	8. (1)	9. (4)	10. (1)
11. (2)	12. (4)	13. (4)	14. (1)	15. (3)	16. (2)	17. (2)	18. (2)	19. 6	20. 24
21. (4)	22. (4)	23. (3)	24. (2)	25. (2)	26. 11	27. 24	28.2	29. 160	30. (1)
31. (1)	32. (1)	33. (1)	34. (2)						

CAT 2017

SHIFT-1

SOLVED PAPER

Answers and Explanations

Verbal Ability and Reading Comprehension (VARC)

1. Option (2) is correct.

The passage talks about history of map and states that it is perhaps surprising that is "only within the last few hundred years that north has been consistently considered to be at the top". This implies that north appearing at the top is more recent phenomenon. The passage further goes on to explain how, historically, other directions were put on the top of maps in different cultures and north was considered a bad direction. He elaborated that the reasons for different people putting north at the top were different from what people think now. So, he is trying to clear certain misconception.

Option (1) is ruled out because the author talks about various reasons behind various methods of map making but he doesn't question them.

Option (3) is wrong. Nowhere the passage analyses the method of map-making. It talks more about the history of the method.

Option (4) is ruled out. Most of the data quoted in the passage are from history, they cannot be misrepresented as a myth.

2. Option (2) is correct.

Paragraph (2) makes it clear that North is where darkness was thought to come from. So, option (1) is eliminated.

Para 4 tells that early Muslim and Christian cultures considered south and east important for religious reasons. So, option (3) and (4) are ruled out.

But nowhere it is mentioned that south was favoured by emperors.

3. Option (2) is correct.

'In Chinese maps, the emperor, who lived in the north of the country was always put at the top of the map, with everyone else, his loyal subjects, looking up towards him'. From paragraph 3 the line explains the reason explicitly.

Options (1) and (4) are eliminated outright. The passage mentions that the Chinese compasses pointed to magnetic south and that south was considered a more desirable direction.

Option (3) is factually incorrect.

4. Option (3) is correct.

Options (1), (2), and (4) can be easily eliminated. From the line, 'European explorers like Christopher Columbus and Ferdinand Megellan who were navigating by the North Star.'; options (2) and (4) are ruled out. From the last paragraph we can infer that the trend of north-up maps was not set by the explorers. So, option (1) is ruled out.

From the lines, "When Columbus describes the world it is in accordance with east being at the top," he says "Columbus says he is going towards paradise, so his mentality is from a medieval mappa mundi." Option (3) can be inferred.

5. Option (4) is correct.

The author doesn't give any reason of why north featured to the top of the map. He discussed all the options and refuted them. (1) and (2) are refuted in the last paragraph where the author denies usage of compass and says that though it is tempting to put it down to European explorers like Christopher Columbus and Ferdinand Megellan who were navigating by the North Star, 'these early explorers didn't think of the world like that at all.'As per the author, East was placed at the top of Christian maps. So option (3) is ruled out.

6. Option (1) is correct.

From the fourth paragraph, 'In ancient Egyptian times the top of the world was east, the position of sunrise.', option (1) can be derived.

7. Option (1) is correct.

In the first paragraph the author talks about the printing press and states that "This was the internet of its day". In the second paragraph he illustrates that the printing press encouraged reading or offered information in several languages. This idea is summed up in option (1).

8. Option (4) is correct.

From the second paragraph, "Medical information passed more freely and quickly, diminishing the sway of quacks" and "Gutenberg's brainchild broke the monopoly that clerics had on scripture", option (2) can be derived. Hence, option (2) is ruled out.

From the same paragraph, "And later, stirred by pamphlets from a version of that same press, the American colonies rose up against a king and gave birth to a nation" and "it's hard to imagine the French or American revolutions without those enlightened voices in print", option (1) can be derived. Hence, option (1) is ruled out. From the last two lines of the first paragraph "Before the invention of the printing press, it used to take four monks up to a year to produce a single book. With the advance in movable type in 15th century Europe, one press could crank out 3,000 pages a day", option (3) can be inferred.

Option (4) is neither stated nor implied anywhere in the passage.

9. Option (3) is correct.

From the fifth paragraph, 'Not long after Steve Jobs introduced his iphone, he said the bound book was probably headed for history's attic.', option (3) is evident.

10. Option (3) is correct.

From the lines, 'The hope of the iPhone, and the internet in general, was that it would free people in closed societies. But the failure of the Arab Spring, and the continued suppression of ideas in North Korea, China and Iran, has not borne that out...', it is clear that iPhone has not brought the kind of technical revolution he was expecting.

11. Option (2) is correct.

From the lines, 'the printing press opened more minds than anything else...it's hard to imagine the French or American revolutions without those enlightened voices in print', it is clear that the author wants to establish importance of printing press in spreading information quickly. This is expressed in option (2).

12. Option (2) is correct.

The author concluded the passage with the lines, 'I'm not sure if the world changed for the better with the iPhone — as it did with the printing press — or merely, changed.' This tells us that in comparison to printing press, new technology has done nothing to make the society more liberated or enlightened.

The passage doesn't compare advantages or disadvantages of the new technology. So, option (1) is ruled out.

Option (3) and option (4) are eliminated because they contradict the information given in the passage.

13. Option (3) is correct.

Option (1) is a close choice. But the passage focuses on malls serving as public squares and being the hub of the social life of middle-class America. The passage doesn't tell how mall closures has affected the economic situation of middle-class Americans. So, option (1) is ruled out.

The passage doesn't talk about disadvantages of mall. So, option (2) is eliminated.

Option (4) is incorrect because it focuses upon a narrow aspect discussed in the passage. Hence, the answer is malls used to perform a social function that has been lost. The central idea of the passage is reflected in option (3).

14. Option (1) is correct.

Option (2) states that the malls and distribution centres are located in the same area. This is correct to certain extent but the passage highlights that distribution centres are replacing malls. So, option (2) is ruled out.

Option (3) is eliminated because nowhere the passage suggests that Amazon is helping brands to go online. Option (4) is eliminated because change in shopping habit is stated in the last paragraph, but the question is about the second paragraph.

Option (1) captures the author's intent of expressing ironical situation that the new work place is situated near the old work place.

15. Option (2) is correct.

"Real estate developers *once* stumbled over themselves to court the brand-name outlets", means they sought after the brand names once but now they don't. It's suggested in option (2). The other three options are outside the scope of the question.

16. Option (3) is correct.

Paragraph 6 states, 'That mall was an ecosystem unto itself, a combination of community and commercialism peddling everything you needed and everything you didn't...' From this line it is clear that malls were not only the place of shopping but also community gathering. Hence, option (3) is the correct answer. Options (1), (2) and (4) do not answer the question correctly.

17. Option (4) is correct.

'It was the home of first jobs and blind dates, the place for family photos and ear piercings, where goths and grandmothers could somehow walk through the same doors and find something they all liked'. The line indicates the malls were places for social gathering and interactions which is reflected in option (4).

18. Option (1) is correct.

Option (3) and option (4) can be out-rightly eliminated.

The author mentions, 'Perfume clouds in the department stores' in order to evoke memory of mall by giving its picturesque description which is given in option (1).

Option (2) is factually correct but does not explain why the author talks about the sight and smell of malls. So, option (2) is eliminated.

19. Option (3) is correct.

In the last paragraph, Ehrlich and Raven asserted that 'isolation and gene flow were less important to evolutionary divergence than natural selection', one can select option (3) as the correct answer.

20. Option (2) is correct.

You have to select the option which is not true according to the passage. From the third paragraph, "Isolation and gene flow were less important to evolutionary divergence than natural selection', you can infer that gene flow is important for evolutionary divergence.

The passage mentions that there were three groups of checkerspot butterflies 'that rarely interacted despite their very close proximity'. From this option (4) can be inferred.

Option (3) can be inferred from the second line of the first paragraph. Hence, option (3) is ruled out.

The passage is about 'speciation' not about 'species diversity'. Option (2) can't be derived from the passage because it talks about 'species diversity'.

21. Option (3) is correct.

The passage is about 'speciation', option (1) talks about evolution, which is too broad to select as answer. So, option (1) is ruled out.

Option (2) can be eliminated outright because it is not stated or hinted in the passage.

Option (4) is ruled out because the butterfly is used to elaborate the main idea of the passage and it is not the primary focus of the passage.

The author explains the contrasting views of the scientists to show that specification is a debated topic.

22. Option (3) is correct.

Option (1) and option (2) are ruled out because they are factually not supported by the passage. Option (4) is too negative to select as the answer. The passage talks about expenditure in the first paragraph to create a background of the main idea of the passage. So, option (4) is ruled out.

The passage says that whether host cities accrue economic benefits 'depends, but 'trick is converting several billion dollars in operating costs during the 17-day fiesta of the Games into a basis for long-term economic return'.

23. Option (1) is correct.

The passage doesn't suggest all Olympic avenues are far from the city centre and without easy access. So, option (2) is eliminated.

The passage doesn't say that the authorities do not adapt them to local conditions it merely mentions that the facilities 'require a conversion plan for future use'. So, option (3) is ruled out.

Nothing about facilities becoming outdated is mentioned in the passage. So, option (4) is eliminated.

From the second paragraph, 'The facilities benefit is dubious at best for buildings such as velodromes or natatoriums and problematic for 100,000-seat Olympic stadiums. The latter requires a conversion plan for future use, the former are usually doomed to near vacancy', we can infer that maintenance of such a huge structure is an expensive option.

24. Option (4) is correct.

From the line, 'Even if they have future use, are they the best use of precious urban real estate?'. Option (1) can be derived. So, option (1) is ruled out.

Option (2) can be derived from: "Residential areas often are razed and citizens relocated ". So, option (2) is eliminated.

From the last line of the paragraph, 'There are, after all, other productive uses that can be made of vanishing fiscal resources'. Option (3) can be inferred. So, option (3) is also ruled out.

Option (4) is not mentioned in the passage.

25. Option (3) is correct.

The author asserts that a classic is one which provides access to radically different forms of human consciousness.

Option (1) is contradictory to the paragraph. It says that a classic should focus on unified human experience. But the passage says classic focuses on radically different forms of human consciousness. Therefore, option (1) is eliminated. Option (2) is ruled out since it states that a classic focuses on common humanity.

Option (4) is also eliminated because it states the exact opposite of what is stated in the paragraph. The author is of the view that a classic should go beyond providing a unified human experience and expose one to radically different forms of human consciousness. Only option (3) captures the essence of the given paragraph.

26. Option (3) is correct.

Option (1) talks 'different skill profiles', which is not there in the passage. So, option (1) is ruled out.

Option (2) and option (4) are eliminated because they focus upon the key element that Indian text should be left to Indian translators.

The paragraph asserts that in translations, the interpretation of cultural elements is a big challenge, not the quality of the language. And because for an Indian it is easier to learn the English language than it is for a Briton to understand Indian culture, translation of Indian texts is better done by Indians. Option (3) encompasses the idea of the paragraph.

27. Option (3) is correct.

Option (1) is eliminated because it says Harvey is unrelated to global warming. This is factually wrong.

Option (2) is ruled out. It distorts the facts mentioned in relation to Clausius-Clapeyron equation in the paragraph.

Option (4) is eliminated because it focuses upon Harvey whereas the paragraph is generic in nature.

The paragraph states that because of melting glaciers, the seas expand in volume and because

of global warming, they evaporate more easily and the warm air above the seas holds more water vapour. This leads to wetter and more powerful storms. Option (3) summarises this aptly.

28. Correct answer is [54132].

Sentence (5) is a general statement and it conveys the overarching idea of the paragraph: tradition and innovation. So, it is an opening sentence. Sentence (41) is a pair: Sentence (4) asserts that traditions are not handed down unchanged; Sentence (1)followed it by explaining what that 'handing down' involves. Sentence (3) follows Sentence (1), because it tells that every generation selects what is required from the past to make innovations. Sentence (32) is also a pair: Sentence (2) adds to the idea mentioned in Sentence (3), stating that the selection is apparent when Western scholars have worked on the Indian past.

29. Correct answer is [15243].

Sentence (1) introduces the topic- gene editing and a specific disease where the process has been used effectively. Sentence (5) adds to Sentence (1) by mentioning the names of the specific genetic mutation that scientists have fixed. Sentence (5) is the only sentence that names the disease so, Statement (2), which starts with 'the cardiac disease' follows Statement (5). Statement (4) states the causes of the disease mentioned in statement (2). So, (4) follows (2). And (3) explains the effect of the correction of this genetic mutation and concludes the paragraph.

30. Correct answer is [54123].

Sentence (5) introduces the topic of the paragraph: the disease – black plaque and its impact on migration. (5) mentions about a DNA study and (4) explains the findings of the study. So, (5) follows (5). 1 should follow (5) as 'the study' mentioned in 1 refers to the analysis of skeletons mentioned in the statement (4). (2) and

(3) are related to the ages of skeletons. (2) talks about the oldest sample and (3) concludes by claiming this could have been the reason for mass exodus.

31. Correct answer is [32145].

Sentence (3) is the obvious opener, which is followed by (2). (2) talks about framing the vision, the vision is stated in (3). Sentence (1) elaborates the idea of Sentence (2) by talking of the visual turn in social media. (4) elaborates how Facebook has accentuated our announcing instinct; so, sentence (4) follows (1). And (5) concludes the paragraph.

32. Option (3) is correct.

This is a bit tricky question. At first glance it seems that all the sentences are about the same topic, but after careful reading we come to know that the paragraph is all about babies understanding of language and their reactions. Sentence (1) introduces the topic signs of understanding babies show while reacting to speech, which is reinforced by sentence (2). Followed by sentence (4) and (5), but sentence (3) talks about when babies begin to show understanding, which is a slightly a different idea.

33. Option (4) is correct.

The paragraph is about the study of the impact of exercise on our brain cells by neuroscientists. Sentence (1) starts the paragraph by introducing the topic. Sentence (2), (3) and (4) elaborate this topic. Only sentence (4) gives a generic view about the relation of mind and body.

34. Option (1) is correct.

The subject of this paragraph is lost water of mars. Sentence 5 initiates the topic by talking about two findings related to the subject matter. The first one tells how mars lost its water and the other talks about remaining water. Rest of the sentences explain these studies. (2) and (4) elaborate how mars lost its water and (3) tells where the remaining water is. Only sentence (1) is a misfit in the sequence.

Data Interpretation and Logical Reasoning (DILR)

For solutions 1 to 4:

Preparation time for a burger = 10 minPreparation time for a ice cream = 2 min

Client no.	Time	Order
1	10:00 a.m.	1 burger, 3 portion of fries, 1 ice cream
2	10:05 a.m.	2 portion of fries, 1 ice cream
3	10:07 a.m.	1 burger, 1 portion of fries

1. Option (2) is correct.

Client 1 order:

1burger, 3	portion of frie	s, 1 ice-cream
\downarrow° 10 min	↓ 5 min	↓ 2 min

As order placed at 10:00 a.m. and maximum time taken for burger which is 10 min.

- So, order will be completely served at 10:10 a.m.
- 2. Option (3) is correct. As first order will be done at 10:10 a.m.

Second order: 2 fries and 1 ice-cream means that will done at 10:15 a.m.

Third order: 1 burger and 1 portion of fries already done with 10 min II order

Mean time when III^{rd} order is complete = 10:25 a.m.

3. Option (1) is correct.

Ist order:

1 burger, 3 portion of fries 1 ice-cream $\downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \downarrow \qquad \qquad \downarrow \qquad \qquad 10 \min \qquad 5 \min \qquad 2 \min$ $2\dot{min}$

IInd order: 2 portion of fries, 1 ice-cream ý 5min \downarrow 2 min

As shown when 1 burger prepared, meanwhile twice 3 portion of fries prepared and both icecream as well.

So, at 10:10 a.m. IInd order will be completed.

For solutions 5 to 8:

Order 1:

1 burger, 3 portion of fries, 1 ice-cream \downarrow \downarrow \downarrow \downarrow 10 min 5 min 2 min Anish can start working in Ist order. As second order placed at 10:05 a.m. of 2 portion of fries and 1 ice-cream. Bani can work on fries and ice cream at 10:05 a.m. As employees are allowed to process multiple order at a time. When Anish started making of Burger. Same time Bani started for ice-cream and meditate 10:02 a.m. When second order place Bani started again for ice-cream at 10:05. Means Bani was free for 3 min. [From 10:02 a.m. to 1:05 a.m.]. IIIrd order placed at 10:07 a.m. and Bani will start immediately working on the burger. He will finish it by 10:17 a.m. Anish finished the burger at 10:10. Only he is free for 7 min [from 10:10 to 10:17] Thus exactly one person is free for 10 min.

Total students surveyed =
$$30000$$

Kids from NE = $150 \times 50 = 7500$
Kids from W = $250 \times 50 = 12500$
Kids from S = $200 \times 50 = 10000$

Students studied in primary school = $30000 \times \frac{55}{100} = 16500$

Students studied in private school = $30000 \times \frac{37}{100} = 11100$

Students did not go to school =
$$30000 \times \frac{8}{100} = 2400$$

Also given that:

	G	Р	0	Total
NE	4200	500	300	5000
W	4200	1900	1200	7300
S	5100	300	300	5700
Total	13500	2700	1800	18000

From the table:

NE: The mothers of 5000 students dropped out before completing the primary education.

Means remaining kids	[2500] fro	m NE should have	mothers who cor	npleted	primary	education.
----------------------	------------	------------------	-----------------	---------	---------	------------

W: Students whose mothers completed primary education	= 12500 - 7300 = 5200
S: Students whose mothers completed primary education	= 10000 - 5700 = 4300
Also can be conclude that:	
1. Students in G whose mother completed primary education	= 16500 - 13500 = 3000
2. Students in P whose mother completed primary education	= 11100 - 2700 = 8400
3. Category O students whose mother completed primary education	= 2400 - 1800 = 600
Point 1:	

In S, 60% surveyed kids in G.

Therefore, 6000 kids in S must be from G.

Point 2:

In NE, among the O kids, 50% had mothers who had dropped out before completing primary education. Give 300 students whose mothers dropped from primary education.

Means 300 students whose mothers completed primary education.

	G			Р		0	
	Dropped	Completed	D	C	D	С	7500
NE	4200	1050	500	1150	300	300	12500
W	4200	1050	1900	3850	1200	300	10000
S	5100	900	300	3400	300	0	10000
Total	13500	3000	2700	8400	1800	600	30000

5. Option (1) is correct.

As seen from table:

In S total students studying in P = 3400 + 300

$$= 3700$$

Required percentage
$$= \frac{3700}{10000} \times 100 = 37\%$$

Option (1) is correct. 6.

From last column of table, number of mothers, who completed primary education, were not in school = 300.

7. **Option (1) is correct.**

Initially number of kids who were out of school

= 2400Number of students out of school

For solutions 9 to 12:

Venn diagram for above 80 percentile students:

Exactly one subject =
$$a + b + c$$

Exactly two subjects = $d + e + f$
Exactly three subjects = $g = 0$ [given]
Total candidates = 200
Point 2: $d + e + f = 150$

2a + e = 4x

$$2a + f = 2x \qquad \dots (ii)$$
$$2a + d = x \qquad \dots (iii)$$

...(i)

a = b = c

$$6a + [d + e + f] = 7x$$

$$6a + 150 = 7x$$

Also, 6a + 150 must be divisible by 7.

So, possible value of a = 3 or 10

Then, *x* may be 24 or 30.

Two possible Venn diagrams based on *a* and *x* value are as follows:

50% of students who were not in school but

Studying in G now =
$$\frac{50}{100} \times 2400 = 1200$$

the only possible case is:

If 50% of the kids from W (750),

25% of the kids from NE (150),

and 100% of the kids from S (300) are transferred.

Then the total number of kids transferred to G

$$= 750 + 150 +$$

 $= 1200$

300

Number of students transferred to G in W = 750Number of students present in G in W earlier = 5250

So, Total = 6000

8. **Option (1) is correct.**

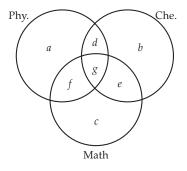
> Already 5100 kids whose mothers had dropped out were in G in S.

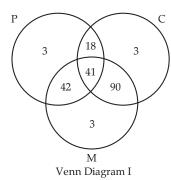
> After transfer, 300 more students will be added to the count.

> So, 5400 students whose mothers had dropped out will be G in S.

> Total number of kids whose mothers dropped in S = 5700

Percentage
$$=\frac{5400}{5700} = 94.73\%$$



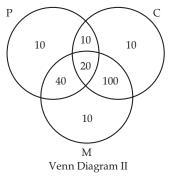


- 9. Option (1) is correct. From both Venn diagrams either 3 or 10 from Physics section.
- **10.** Correct answer is [60]. According to question, Venn diagram I is valid. Total candidate = 20 + 40 = 60
- 11. Correct answer is [170]. According to question, Venn diagram I is valid. \Rightarrow Total candidates here = 200 - 30 = 170

(Individuals exactly)

For solutions 13 to 16:

Tabulation of Given data



12. Option (1) is correct.

Here in question, P should more than 100.

 I^{st} Venn diagram P = 3 + 18 + 41 + 42 = 104

IInd Venn diagram P = 10+10+20+40 = 90

Means Ist is valid in this case:

The students had to sit for the separate test for

BIE = 400 - [18 + 41 + 42] = 299

Scores	S	F	С
1		2	1
2		1	3
3	3	2	4
4	3	1	1
5	2	3	
6	1		1
7	1	1	

Point 1: Amda score = Class score = 7 and identical scores in all three parameters Point 2: Zooma has total score = 17

Point 3: 3 countries, which categorised happy have the highest score in exactly one parameter.

13. Correct answer is [1].

Given that Amda score = 7 and Calla score = 7 and identical in all parameters. Possible score for

- A C
- 4 2 1 4 2 1
- or 3 3 1 3 3 1
- or 5 1 1 5 1 1

[Not possible as frequency of score 1 is not sufficient in table

So, now scores of A in all parameters.

SFC or SFC

4 1 2 3 1 3

So, in both cases Amda's score in F = 1

14. Correct answer is [6].

Given Zooma total score is = 17

Also, given 3 countries are categorised as happy means scored between 14 to 19 and have highest score in one parameter. Means Zooma is one of these three countries.

6 7 4

Hence, Zooma's score in S is 6.

15. Option (2) is correct. Benga score = Delma score = same total score. So, maximum possible score for Benga when 7, 5, 6 added is 18. But at same time then Delma can't score 18.

Same way both can't score 17 & 16. So, both can score 15.

16. Option (2) is correct.

Benga's score = 16

and Delma's score = 15

possible score for Benga = 5, 6, 6

- and for Delma = 7, 5, 3
- But, if Benga scores 7, 3, 6 then Delma can't score 15.

So, to score 13, the distribution can be 5, 6, 3. Hence, maximum 1 country is possible.

For solutions 17 to 20:

17. Option (2) is correct.

The total number of employees = 21Special skilled employee [SE] = 10and Regular skilled employee [RE] = 11As per given condition for 1st month:

	SE	RE	Total
T ₁	4	1	5
T ₂	3	1	4
T ₃	2	2	4
T ₄	1	3	4
T ₅	1	3	4

For 2nd month after exchanging the employees:

		0 0	1 2
	SE	RE	Total
T ₁	1	3	4
T ₂	4	1	5
T ₃	2	2	4
T ₄	2	2	4
T ₅	1	3	4

For 3rd month:

	SE	RE	Total
T ₁	0	4	4
T ₂	1	3	4
T ₃	4	1	5
T ₄	3	1	4
T ₅	2	2	4

For 4th month:

	SE	RE	Total
T ₁	0	4	4
T ₂	1	3	4
T ₃	2	2	4
T ₄	5	0	5
T ₅	2	2	4

For 5th month:

	SE	RE	Total
T ₁	0	4	4
T ₂	0	4	4
T ₃	2	2	4
T_4	4	0	4
T ₅	4	1	5

T2 remain unchanged for 3rd and 4th month and T₄ was never unchanged. So, answer would be (1, 0).

18.	Option (1) is correct. In 3 rd month,
	SE in $T_1 = 0$
	and SE in $T_5^1 = 2$
	So, answer is (0, 2).
19.	Option (2) is correct.
	When challenging project is given, each
	employee gets 40 points.
	When standard project is given, each employee gets 25 points.
	What an employee can earn while working on
	different projects:
	1. 5 standard project + 0 challenging project
	$= 5 \times 25 = 125$
	2. 4 standard project + 1 challenging project
	$= 4 \times 25 + 1 \times 40 = 140$
	3. 3 standard project + 2 challenging project
	$= 3 \times 25 + 2 \times 40 = 155$
	4. 2 standard project + 0 challenging project
	$= 2 \times 25 + 3 \times 40 = 170$
	5. 1 standard project + 4 challenging project
	$= 1 \times 25 + 4 \times 40 = 185$
	6. 0 standard project + 5 challenging project

 $=40 \times 25 = 200$

So, only 150 score is not possible.

20. Option (4) is correct.

Since, Aneek secured 185 credits, he has worked in four challenging projects and one standard project.

- (1) Aneek could have worked in T_1 in 1^{st} month (in challenging project), T_2 in 2^{nd} month (in challenging project), T_3 in 3^{rd} month (in challenging project), T_4 in 4th month (in challenging project) and 5th month (in standard project). Hence, this is possible.
- (2) Aneek could have worked in T_1 in 1st month (in challenging project), T_2 in 2^{nd} month (in challenging project), T_4 in 3^{rd} month (in standard project), T_4 in 4^{th} month (in challenging project) and T₅ in 5th month (in challenging project). Hence, this is possible.
- (3) Aneek could have worked in T_2 in 1st month (in standard project), $T_{\rm 2}$ in $2^{\rm \bar{n}d}$ month (in challenging project), T_3 in 3^{rd} month (in challenging project), T_4 in 4^{th} month (in challenging project) and T_5 in 5^{th} month (in challenging project). Hence, this is possible.
- (4) Aneek could have worked in T_1 in 1^{st} month (in challenging project). He can work in T_1 or T_{5} in the 2nd month. In either case, he cannot work in T₃ without working in T₂ first. If we assume, he worked in T_3 in the 1st month, he could not have worked in four teams in the five months. Similarly, we can rule out the other possibilities. Hence, this is the answer.

For solutions 21 to 28:

Individual A can reach individual B if all three conditions meets.

- 1. A and B are in same row/column.
- 2. A is at lower height than B.
- 3. If there is any individual seated between A and B at height.

6	1	2	4	3
9	5	3	2	8
7	8	4	6	5
3	9	5	1	2
1	7	6	3	9

Tabulation form with an individual reachability:

	6	, 3	d	0	с	1	4	3	3	0
reach	9	4	5	2	3	2	2	0	8	5
6 can reach 3 Persons	7	1	8	4	4	1	6	6	5	1
	3	1	9	4	5	3	1	0	2	1
	1	0	7	2	6	2	3	1	9	6

21. Option (3) is correct.

As in table there are total 7 people who can reach just one individual.

22. Option (4) is correct.

According to point (2), any individual can reach only them who are smaller than him. So, any individual at a platform of height 1 m in this layout cannot be reached by anyone.

23. Option (3) is correct.

As we can see in the table that in 4th column two individuals can't be reached by anyone.

24. Option (3) is correct.

While checking all the options, only option (3) is true.

Each row has at least two individuals who can be reached by an equal number of individuals.

25. Option (3) is correct.

A number of selection of 2 cities out of 10 cities ${}^{10}C_2 = 45$ Now for travelling in these 2 cities, Minimum 4 flights are required.

1 to go from A to B,

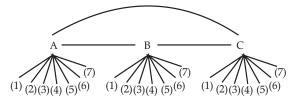
- 1 to go from B to A,
- and 1 to return A,
- and 1 to return B.

So, minimum number of flights required

$$= 4 \times 45 = 180$$

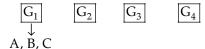
26. Option (3) is correct.

Let 3 hub cities = A, B, C



Total flights required = $3 [7 \times 4] + [3 \times 4] = 96$

27. Correct answer is [40].



Also given; $A \rightarrow G_2$ $B \rightarrow G_3$ $C \rightarrow G_4$ Flight required for both cities in $G_1 = 3 \times 4 = 12$ Flight required for A to any city in

 $G_2 = 3 \times 4 = 12$ Flight required for B to any city in

$$G_3 = 2 \times 4 = 8$$

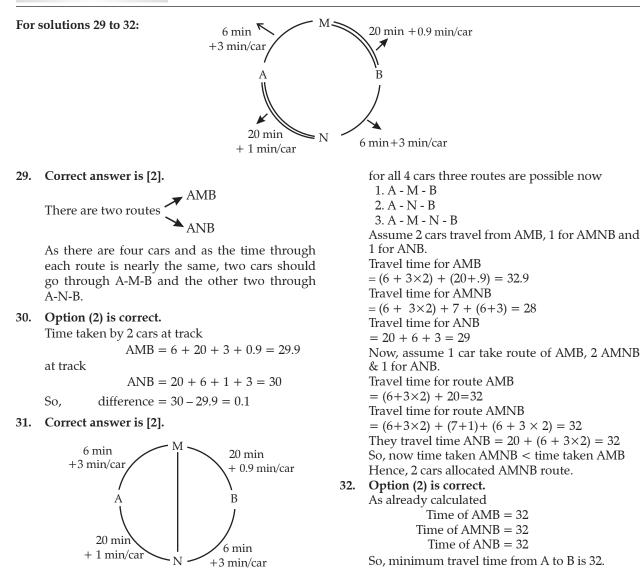
Flight required for C to any city in

$$G_4 = 2 \times 4 = 8$$

Total flights =
$$12 + 12 + 8 + 8 = 40$$

28. Correct answer is [4].

As per conditions given in the question, the only reduction will be due to number of flights stuffing down from A to C. So, total count = 4



Quantitative Aptitude (QA)

1. Correct answer is [20]. Let Barun's age = 5x years And Arun's age = 2x years Let after *y* years, Arun's age will be half of the Barun's age. According to the question,

$$2x + y = \frac{1}{2}(5x + y)$$
$$4x + 2y = 5x + y$$
$$y = x$$

 \Rightarrow \Rightarrow

So, 2x and 5x will be 3x and 6x respectively after y years.

Hence, required percentage increase

 $=\frac{6x-5x}{5x} \times 100 = 20\%$

2. Correct answer is [15].

> Let, the rate of work of a person be 1 unit/day. Hence, the total work = 120.

It is given that on first day, one person works, on the second day two people work and so on. The work done on day 1, day 2, ... will be 1, 2, 3,

..., respectively.

The sum should be equal to 120. If *n* days are required.

Then,
$$\frac{n(n+1)}{2} = 120.$$

On solving, we get n = 15. Hence, it takes 15 days to complete the work.

3. Correct answer is [11].

It is given that the maximum weight limit is 630 kg. The lightest person's weight is 53 kg and the heaviest person's weight is 57 kg.

In order to have maximum people in the lift, all the remaining people should be of the lightest weight possible, which is 53 kg.

Let there be *n* people.

53 + n(53) + 57 = 630 $n \approx 9.8$. \Rightarrow Hence, 9 people are possible. Therefore, a total of 9 + 2 = 11 people can use the elevator.

4. Correct answer is [20]. Absolute difference in time = 10 + 10 = 20 mins

$$=\frac{1}{3}h$$

Hence, if D be the distance we can say

$$\frac{D}{12} - \frac{D}{15} = \frac{1}{3}$$

$$\Rightarrow \qquad \qquad \frac{D}{60} = \frac{1}{3}$$

$$\Rightarrow \qquad \qquad D = \frac{60}{3} = 20 \text{ km}$$

5. Correct answer is [70000].

Ravi invests 50x in fixed deposits. 30% of 50x, which is 15x is invested in stocks and 35x goes to savings bank. It is given

85x = 59500x = 700100x = 70000Hence, So, Ravi's total monthly savings = ₹ 70000

Option (4) is correct. 6.

Let the retail price be M and cost price be C. $\therefore 0.85 \text{ M} = 1.02 \text{ C}$ \Rightarrow M = 1.2 C

If he wants 20% profit he has to sell at 1.2C, which is equal to the retail price.

7. **Option (2) is correct.**

If speed of river = xSpeed of boat = yDistance = dUpstream speed y - x Downstream speed = y + x

Time taken =
$$t$$

Hence,
$$t = \frac{d}{y+x} + \frac{d}{y-x} \Rightarrow t = \frac{2yd}{y^2 - x^2}$$

If, speed of boat = $2y$

Then,

Hence,

Time =
$$\frac{t}{t}$$

d 2y + x

$$t = \frac{16ya}{4y^2 - x^2}$$

16*yd*

2y - x

$$\frac{2yd}{y^2 - x^2} = \frac{16yd}{4y^2 - x^2}$$
$$\frac{1}{y^2 - x^2} = \frac{8}{4y^2 - x^2}$$

or
$$7x^2 = 4y^2$$

 $\therefore \qquad \frac{y}{x} = \frac{\sqrt{7}}{2}$

8. **Option (1) is correct.**

> Given, C1:C2:C3 = 9:10:8... (i) C2:C4:C5 = 18:19:20... (ii) Multiply (i) by 9 and (ii) by 5, we get, C1:C2:C3 = 81:90:72C2:C4:C5 = 90:95:100Therefore, C1 : C2 : C3 : C4 : C5 = 81 : 90 : 72 :95:100Given, 100x - 81x = 19 cr. $x = \mathbf{E}1$ cr. \rightarrow Hence, total profit = 100x + 95x + 72x + 90x + 81x = 438x= ₹438 cr.

Option (4) is correct. 9.

Let the number of girls be 2x and number of boys be x. Girls getting admission = 0.6xBoys getting admission = 0.45xNumber of students not getting admission = 3x - 0.6x - 0.45x = 1.95x(1.95r)Р

Percentage =
$$\left(\frac{1.95x}{3x}\right) \times 100 = 65\%$$

10. Option (1) is correct.

The ratio of L, S, J for popcorn = 7:17:16Let them be 7*x*, 17*x* and 16*x*. The ratio of L, S, J for chips = 6: 15: 14Let them 6*y*, 15*y* and 14*y*. Given, 40x = 35y = 280(Assume) Hence, x = 7 y = 8, Hence, the ratio of jumbo popcorn and jumbo chips $16 \times 7 : 14 \times 8 = 1 : 1$

11. Option (2) is correct.

Let, the cost of good mangoes be 200 per kg. The cost of medium mangoes be 100 per kg. C.P. of good mangoes = $80 \times 200 = 16000$ C.P. of medium mangoes = $40 \times 100 = 4000$ Total C.P. = 20000His selling price = $0.9 \times 200 = 180$ Therefore, total revenue generated by selling all the mangoes = $120 \times 180 = 21600$ Hence, the profit $\% = \frac{21600 - 20000}{20000} \times 100 = 8\%$

12. Option (4) is correct.

Let the cost price be C and the marked price be M. Given,

$$0.6M = 1.2C$$

 $M = 2C$

C.P. of 60 toys = 60CNow, only 50 are remaining. Hence, If *d* is % discount, then

$$M\left(\frac{1-d}{100}\right) \times 50 = 72C$$
$$\Rightarrow \qquad \frac{1-d}{100} = 0.72$$
$$\Rightarrow \qquad d = 28\%$$

Shortcut Method:

Let the M.P. of 60 toys = 60x. As she gave 40% discount C.P. = 36x. Now after 10 toys are destroyed, C.P. of 50 toys = 50x. So she should give a discount of 14x, now.

Discount
$$\% = \frac{14x}{50x} \times 100 = 28\%$$

(**Note:** after 10 toys are destroyed the C.P. should remain same and as he wants some amount of profit S.P. should remain same too).

13. Option (4) is correct.

As we know if $a^2 = 9 a = \pm 3$ Note: Square root of a number is always +ve $\sqrt{9} = 3$ but if $a^2 = 9$ $\Rightarrow a = \pm 3$ Hence, for the first relation, a + 3 = 3b...(i) a + 3 = -3b...(ii) For the second relation, a - 1 = 2(b - 1)...(iii) a - 1 = 2(1 - b)...(iv) we have to solve (i) and (iii), (i) and (iv), (ii) and (iii), (ii) and (iv). Solving (i) and (iii), we get, a = 3 and b = 2, (not possible) Solving (i) and (iv). we get, b = +1.2, (not possible). Solving (ii) and (iii) we get, b = 0.4, (not possible). Solving (ii) and (iv), we get, a = 15 and b = -6 which is possible. Hence, $\frac{a^2}{b^2} = 25:4$

14. Option (1) is correct.

Let, the average score of the boys and girls be 'b' and 'g', respectively. **Mid-semester:** Average score of boys = b

average score of girl, g = b + 5Average score of the whole class

$$=\frac{[20b+30(b+5)]}{50} \qquad \dots (i)$$

Final examination:

Let, the average score of boys be 'B', then the average score of girls, g = b + 2Average score of the whole class

$$=\frac{[20B+30(b+2)]}{50}$$
...(ii)

According to the question,

$$\frac{[20B+30(b+2)]}{50} - \frac{[20b+30(b+5)]}{50} = 2$$

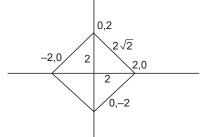
$$\Rightarrow \qquad 20B = 20b+190$$

$$\Rightarrow \qquad B = b+9.5$$

So, average of boys increases by 9.5.

15. Option (3) is correct.

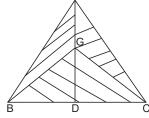
The area of the closed region bounded is given by the equation, |x| + |y| = 2. Taking x = 0 or y = 0 for finding the coordinates. The coordinates we obtain are as follows; (2, 2), (-2, 2), (2, -2) and (-2, -2)



On joining these points, a square can be drawn whose diagonal is 4 units.

So, sides of the square = $2\sqrt{2}$ units

Hence, area of square = $2\sqrt{2} \times 2\sqrt{2} = 8$ sq. units **16. Option (2) is correct.**



Given that:

 \triangle ABC with sides of lengths AB = 40 ft, BC = 25 ft and AC = 35 ft, a triangular portion GBC is cut off where G is the centroid of \triangle ABC. Here \triangle GBC is the one third area of the triangle.

We can join AG and GD which is the median. Each of the shaded triangle has the same area and therefore the remaining area is two-thirds of Δ ABC.

Semi perimeter of
$$\triangle ABC = \frac{40 + 25 + 35}{2} = 50$$
 ft
So, area of $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$

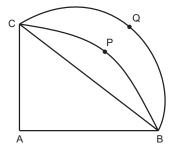
$$= \sqrt{50(50 - 40)(50 - 25)(50 - 35)}$$

$$= \sqrt{50 \times 10 \times 25 \times 15} = 250\sqrt{3}$$
 sq. feet

So, area of remaining portion of $\triangle ABC$

$$=\frac{2}{3} \times 250\sqrt{3} = \frac{500}{\sqrt{3}}$$
 sq. feet

17. Option (2) is correct.



AB = AC = 6 cm. Thus, BC = $\sqrt{6^2 + 6^2} = 6\sqrt{2}$ cm

The required area = Area of semi-circle BQC – Area of quadrant BPC + Area of triangle ABC Area of semicircle BQC

Diameter BC = $6\sqrt{2}$ cm

Radius =
$$\frac{6\sqrt{2}}{2} = 3\sqrt{2}$$
 cm
Area = $\frac{\pi r^2}{2} = \pi \times \frac{(3\sqrt{2})^2}{2} = 9\pi$

Area of quadrant BPC

Area =
$$\frac{\pi r^2}{4} = \pi \times \frac{(6)^2}{4} = 9\pi$$

Area of triangle ABC

Area =
$$\frac{1}{2} \times 6 \times 6 = 18$$

The required area = Area of semi-circle BQC – Area of quadrant BPC + Area of triangle ABC = $9\pi - 9\pi + 18 = 18$

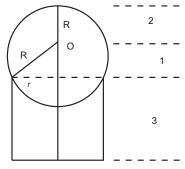
18. Option (2) is correct.

Ratio of volumes of 5 smaller cubes and original big one = 1:1:8:27:27:64Ratio of sides = 1:1:2:3:3:4Ratio of areas = 1:1:4:9:9:16

The sum of the areas of the 5 smaller cubes is 24 parts while that of the big cube is 16 parts.

The sum is
$$\left\lfloor \frac{(24-16)}{16} \right\rfloor \times 100 = 50\%$$
 greater.

19. Correct answer is [6].



Height of the cylinder, h = 3

Volume =
$$9\pi$$

 $\pi r^2 h = 9\pi$
 $r = \sqrt{3}$

The radius of the ball, R = 2

The height of O, the centre of the ball, above the line representing the top of the cylinder is 1.

Therefore, the height of the topmost point of the ball from the base of the cylinder

$$= h + 1 + R$$

= 3 + 1 + 2
= 6

20. Correct answer is [24].

The length of the altitude from A to the hypotenuse will be the shortest distance. This is a right triangle with sides 3:4:5.

Hence, the hypotenuse = $\sqrt{15^2 + 20^2} = 25$ km. Length of the altitude = $15 \times \frac{20}{25} = 12$ km

Time taken = $\frac{12}{30} \times 60 = 24$ minutes

21. Option (4) is correct.

We know that $\log_3 x = a$ and $\log_{12} y = a$ Hence, $x = 3^a$ and $y = 12^a$ Therefore, the geometric mean of x and y equals $\sqrt{x \times y}$

This equals $\sqrt{3^a \times 12^a} = 6^a$ Hence, G = 6^a or, $\log_6 G = a$ **22. Option (4) is correct.**

We know that $x^2 - x - 1 = 0$ Therefore, $x^4 = (x + 1)^2 = x^2 + 2x + 1$ = x + 1 + 2x + 1 = 3x + 2Solving, we get Hence, $2x^4 = 6x + 4$ $x = \frac{1 + \sqrt{5}}{2}$

Put the value of *x* and we get the expression to be equal to $3\sqrt{5} + 7$.

23. Option (3) is correct.

:..

 $\log_{0.008} \sqrt{5}$ can be written in the terms of five and $\log_{\sqrt{3}} 81$ can be written in the terms of 3.

where
$$\sqrt{5} = 5^{1/2}$$

$$0.008 = \frac{2^{-1}}{10^{3}} = 5^{-3}$$
$$= \log_{0.008} \sqrt{5} + \log_{\sqrt{3}} 81 - 7$$
$$= \frac{\log_{5} \sqrt{5}}{\log_{5} 0.008} + \frac{\log_{3} 81}{\log_{3} \sqrt{3}} - 7$$
$$= \frac{\frac{1}{2}}{-3} + \frac{4}{1} - 7$$

 \Rightarrow

$$= \frac{-1}{6} + 1$$
$$= \frac{5}{6}$$

24. Option (2) is correct.

Given,

$$9^{\left(x-\frac{1}{2}\right)}-2^{(2x-2)} = 4^{x} - 3^{(2x-3)}$$
Rearrange:

$$9^{\left(x-\frac{1}{2}\right)} + 3^{(2x-3)} = 4^{x} + 2^{(2x-2)}$$

$$\Rightarrow \qquad 3^{(2x-3)}(3^{2}+1) = 2^{(2x-2)}(2^{2}+1)$$

$$\Rightarrow \qquad 3^{(2x-3)}(10) = 2^{(2x-2)}(5)$$

$$\Rightarrow \qquad 3^{(2x-3)} = \frac{2^{(2x-2)}(5)}{10}$$

$$\Rightarrow \qquad 3^{(2x-3)} = \frac{2^{(2x-2)}}{2}$$

$$\Rightarrow \qquad 3^{(2x-3)} = 2^{(2x-3)}$$

$$\Rightarrow \qquad \frac{3^{(2x-3)}}{2^{(2x-3)}} = 1$$

$$\Rightarrow \qquad \left(\frac{3}{2}\right)^{(2x-3)} = 1$$
Comparing power on, both sides, we get

$$2x-3=0$$

 \Rightarrow

$$x = \frac{3}{2}$$

25. Option (2) is correct.

$$x = 25 + y + z$$

Since, y and z are positive integers, minimum value x can take is 27.

$$27 \le x \le 40$$
$$2 \le y + z \le 15$$

Case 1 - when y = 1, z can take 12 values Case 2 - when y = 2, z can take 12 values Case 3 - when y = 3, z can take 12 values Case 4 - when y = 4, z can take 11 values Case 5 - when y = 5, z can take 10 values Case 12 - when y = 12, z can take 3 values Hence, the number of solutions $= 3 + 4 + 5 + \dots + 12 + 12 + 12$ = 99 values.

$$(n-5)(n-10) - 3(n-2) \le 0$$

$$\Rightarrow \qquad n^2 - 15n + 50 - 3n + 6 \le 0$$

$$\Rightarrow \qquad n^2 - 18n + 56 \le 0$$

$$\Rightarrow \qquad n^2 - 14n - 4n + 56 \le 0$$

$$\Rightarrow \qquad (n-14)(n-4) \le 0$$

$$\Rightarrow \qquad \qquad 4 \le n \le 14$$

⇒ *n* = {4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14} *i.e.*, 11 integers **27. Correct answer is [24].**

Equating
$$f(x) = g(x)$$

we get,

 $x^2 + 10x + n = 0$

Therefore,

$$x = \frac{-5 \pm \sqrt{100 - 4n}}{2}$$

For x to be distinct and real, maximum number n can be is 24.

28. Correct answer is [2].

For the value of given expression to be minimum, the values of *a*, *b*, *c* and d should be as close as possible.

$$\frac{30}{4} = 7.5$$

Since, each one of these are integers so values of *a*, *b*, *c*, *d* should be respectively 8, 8, 7, 7.

On putting these values in the given expression, we get the value to be 2.

29. Correct answer is [160].

There are 5 pairs of diametrically opposite points and the centre O.

If O is not selected, the number of triangles ${}^{10}C_3 = 120$.

If O is selected, the other two points can be selected in $\frac{10(8)}{2}$, i.e., 40 ways.

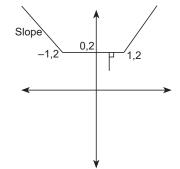
The number of triangles is 160.

30. Option (1) is correct.

Given curve, y = |x - 1| + |x + 1|Here *y* will be entirely positive for given curve.

When $x = \frac{1}{2}$, then $y = \left|\frac{1}{2} - 1\right| + \left|\frac{1}{2} + 1\right| = 2$ x = 1, then y = |1 - 1| + |1 + 1| = 2And x = -1, then y = |-1 - 1| + |-1 + 1| = 2

When x = 1, then y = |-1 - 1| + |-1 + 1| = 2When x > 1 then x - 1 + x + 1 it becomes 2x. When x < 1 then 1 - x - 1 - x it becomes -2x. So, curve can be drawn as shown below.



From the graph obtained we can see that the shortest distance of the point $\left(\frac{1}{2},1\right)$ from the curve will be the perpendicular distance and is equal to 1.

31. Option (1) is correct.

The *n*th term of arithmetic progression can be written as = a + (n - 1)d*a* = first term; *d* = common difference 7th term of A.P. = a + 6d 3rd term of A.P. = a + 2d17th term of A.P. = a + 16d $(a + 6d)^2 = (a + 2d)(a + 16d)$ $a^2 + 12ad + 36d^2 = a^2 + 18ad + 32d^2$ $6ad = 4d^2$ Since d > 0 6a = 4d $\frac{a}{d} = \frac{2}{3}$ 32. Option (1) is correct.

We have been given that a + b + c + d = 7, Total ways of distributing 7 things among 4 people, so that each one gets at least one $= n - 1_{C_{r-1}} = 7 - 1_{C_{r-1}} = 6_{C_r} = 20$

 $7 - 1_{c_{4-1}} = 6_{c_3} = 20$ According to the question, nobody gets more than three erasers.

There are four cases (4, 1, 1, 1) or (1, 4, 1, 1) or (1, 1, 4, 1) or (1, 1, 1, 4), which are not following the given condition.

So, required number of ways = 20 - 4 = 16

33. Option (1) is correct.

Put values of
$$f(3) = \frac{17}{4}$$

Hence,
$$f(f(3)) = f\left(\frac{17}{4}\right) = 3$$

G(3) = 2

34. Option (2) is correct.

$$a_{1} = 3, a_{2} = 7 = a_{n} = 4n - 1, \dots a_{3n} = 4(3n) - 1$$

$$a_{1} + a_{2} + \dots + a_{3n} = \frac{3n(12n + 2)}{2} = 1830$$

$$\Rightarrow \quad n(6n + 1) = 610$$

$$\Rightarrow \quad 6n^{2} + n - 610 = 0$$

$$\Rightarrow \quad (6n + 61) (n - 10) = 0$$

$$\Rightarrow \qquad n = 10 \quad (\because n \text{ is an integer})$$

$$\therefore \quad a_{1}, a_{2} + \dots + a_{n} = 3 + 7 + \dots + [4(10) - 1]$$

$$= \frac{4(10)(11)}{2} - 10$$

$$= 210$$

$$\therefore \quad 210m > 1830$$

$$\Rightarrow \qquad m > \frac{1830}{210} = 8.7$$

The minimum integral value of *m* is 9.