JEE Advanced (2024)

PAPER 2

General Instructions:

SECTION 1 (Maximum Marks: 12)

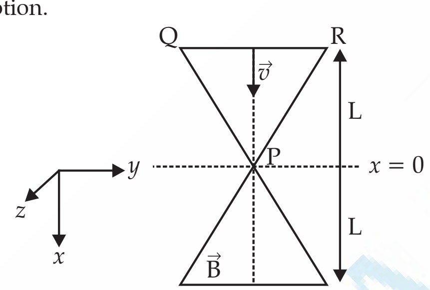
- This section contains **FOUR (04)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY ONE** of these four options is the correct answer.
- For each question, choose the option corresponding to the correct answer.
- Answer to each question will be evaluated **according to the following marking scheme:**

  Full Marks : +3 If **ONLY** the correct option is chosen;

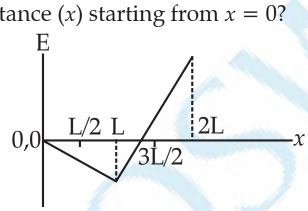
  Zero Marks : 0 If none of the options is chosen (i.e. the question is unanswered);

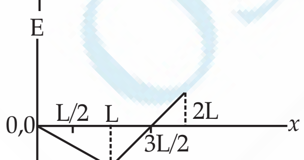
  Negative Marks : –1 in all other cases.

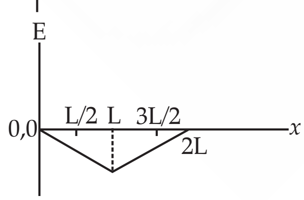
1. A region in the form of an equilateral triangle (in x–y plane) of height L has a uniform magnetic field $\vec{B}$ pointing in the $+z$-direction. A conducting loop PQR, in the form of an equilateral triangle of the same height L, is placed in the x-y plane with its vertex P at $x = 0$ in the orientation shown in the figure. At $t = 0$, the loop starts entering the region of the magnetic field with a uniform velocity $\vec{v}$ along the $+x$-direction. The plane of the loop and its orientation remain unchanged throughout its motion.

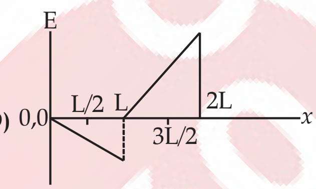


Which of the following graph best depicts the variation of the induced emf (E) in the loop as a function of the distance (x) starting from $x = 0$?

(A) 

(B) 

(C) 

(D) 

2. A particle of mass m is under the influence of the gravitational field of a body of mass M(>> m). The particle is moving in a circular orbit of radius r_0 with time period T_0 around the mass M. Then, the particle is subjected to an additional central force, corresponding to the potential energy $V_c(r) = \dfrac{m\alpha}{r^3}$, where α is a positive constant of suitable dimensions and r is the distance from the center of the orbit. If the particle moves in the same circular orbit of radius r_0 in the combined gravitational potential due to M and $V_c(r)$, but with a new time period T_1, then $\dfrac{T_1^2 - T_0^2}{T_1^2}$ is given by

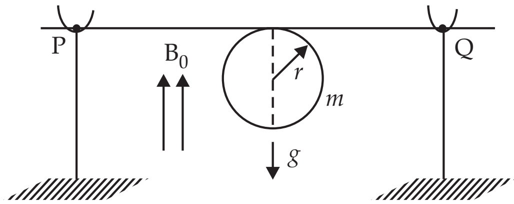
[G is the gravitational constant.]

(A) $\dfrac{3\alpha}{GMr_0^2}$ **(B)** $\dfrac{\alpha}{2GMr_0^2}$ **(C)** $\dfrac{\alpha}{GMr_0^2}$ **(D)** $\dfrac{2\alpha}{GMr_0^2}$

3. A metal target with atomic number Z = 46 is bombarded with a high energy electron beam. The emission of X-rays from the target is analysed. The ratio r of the wavelengths of the K_α-line and the cut-off is found to be $r = 2$. If the same electron beam bombards another metal target with Z = 41, the value of r will be

(A) 2.53 **(B)** 1.27 **(C)** 2.24 **(D)** 1.58

4. A thin stiff insulated metal wire is bent into a circular loop with its two ends extending tangentially from the same point of the loop. The wire loop has mass m and radius r and it is in a uniform vertical magnetic field B_0, as shown in the figure. Initially, it hangs vertically downwards, because of acceleration due to gravity g, on two conducting supports at P and Q. When a current I is passed through the loop, the loop turns about the line PQ by an angle θ given by



(A) $\tan\theta = \frac{\pi r I B_0}{(mg)}$ **(B)** $\tan\theta = \frac{2\pi r I B_0}{(mg)}$

(C) $\tan\theta = \frac{\pi r I B_0}{(2mg)}$ **(D)** $\tan\theta = \frac{mg}{(\pi r I B_0)}$

***General Instructions*:**

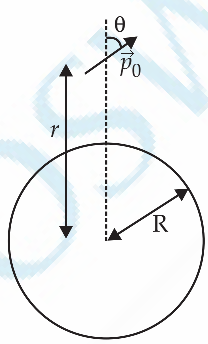
SECTION 2 (Maximum Marks: 12)

- This section contains **THREE (03)** questions.
- Each question has **FOUR** options (A), (B), (C) and (D). **ONLY OR MORE THAN ONE** of these four options is the correct answer.
- For each question, choose the option(s) corresponding to (all) the correct answer(s).
- Answer to each question will be evaluated **according to the following marking scheme:**

Full Marks : +4 **ONLY** if (all) the correct option(s) is(are) chosen;
Partial Marks : +3 If all the four options are correct but **ONLY** three options are chosen;
Partial Marks : +2 If three or more options are correct but **ONLY** two options are chosen, both of which are correct;
Partial Marks : +1 If two or more options are correct but **ONLY** one option is chosen and it is a correct option;
Zero Marks : 0 If none of the options is chosen (i.e., the question is unanswered);
Negative Marks : –2 in all other cases.

- For example, in a question, if (A), (B) and (D) are the ONLY three options corresponding to correct answers, then
choosing ONLY (A), (B) and (D) will get +4 marks;
choosing ONLY (A) and (B) will get +2 marks;
choosing ONLY (A) and (D) will get +2 marks;
choosing ONLY (B) and (D) will get +2 marks;
choosing ONLY (A) will get +1 mark;
choosing ONLY (B) will get +1 mark;
choosing ONLY (D) will get +1 mark;
choosing no option(s) (i.e., the question is unanswered) will get 0 marks; and
choosing any other combination of options will get –2 marks.

5. A small electric dipole $\vec{p}_0$, having a moment of inertia I about its center, is kept at a distance r from the center of a spherical shell of radius R. The surface charge density σ is uniformly distributed on the spherical shell. The dipole is initially oriented at a small angle θ as shown in the figure. While staying at a distance r, the dipole is free to rotate about its centre.



If released from rest, then which of the following statement(s) is(are) correct?

[ε_0 is the permittivity of free space.]

(A) The dipole will undergo small oscillations at any finite value of r.

(B) The dipole will undergo small oscillations at any finite value of $r > R$.

(C) The dipole will undergo small oscillations with an angular frequency of $\sqrt{\frac{2\sigma p_0}{\varepsilon_0 I}}$ at $r = 2R$.

(D) The dipole will undergo small oscillations with an angular frequency of $\sqrt{\frac{\sigma p_0}{100\varepsilon_0 I}}$ at $r = 10R$.

6. A table tennis ball has radius $\frac{3}{2}\times 10^{-2}$ m and mass $\frac{22}{7}\times 10^{-3}$ kg. It is slowly pushed down into a swimming pool to a depth of $d = 0.7$ m below the water surface and then released from rest. It emerges from the water surface at speed v, without getting wet and rises up to a height H. Which of the following option(s) is(are) correct?

[Given: $\pi = \frac{22}{7}$, $g = 10$ m s^{-2}, density of water = 1×10^3 kg m^{-3}, viscosity of water = 1×10^{-3} Pa-s.]

(A) The work done in pushing the ball to the depth d is 0.077 J.

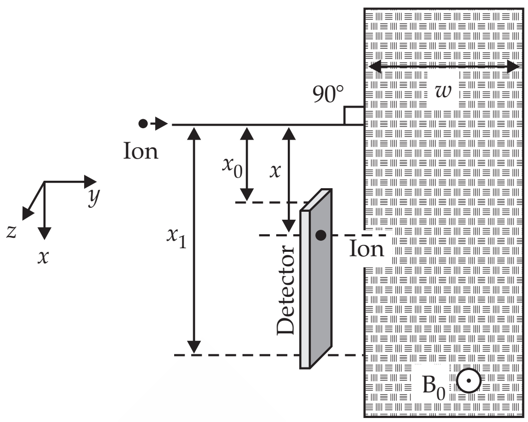
(B) If we neglect the viscous force in water, then the speed $v = 7$ m/s.

(C) If we neglect the viscous force in water, then the height $H = 1.4$ m.

(D) The ratio of the magnitudes of the net force excluding the viscous force to the maximum viscous force in water is $\frac{500}{9}$.

7. A positive, singly ionised atom of mass number A_M is accelerated from rest by the voltage 192 V. Thereafter, it enters a rectangular region of width w with magnetic field $\vec{B}_0 = 0.1\hat{k}$ Tesla, as shown in the figure. The ion finally hits a detector at the distance x below its starting trajectory.

[Given: Mass of neutron/proton $= \frac{5}{3} \times 10^{-27}$ kg, charge of the electron $= 1.6 \times 10^{-19}$ C.]



Which of the following option(s) is(are) correct?

(A) The value of x for H^+ ion is 4 cm.

(B) The value of x for an ion with $A_M = 144$ is 48 cm.

(C) For detecting ions with $1 \le A_M \le 196$, the minimum height $(x_1 - x_0)$ of the detector is 55 cm.

(D) The minimum width w of the region of the magnetic field for detecting ions with $A_M = 196$ is 56 cm.

General Instructions:

SECTION 3 (Maximum Marks: 24)

- This section contains **SIX (06)** questions.
- The answer to each question is a **NON-NEGATIVE INTEGER**.
- For each question, enter the correct integer corresponding to the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- Answer to each question will be evaluated **according to the following marking scheme:**

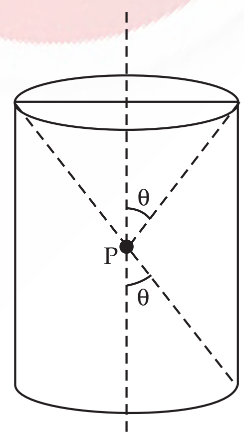
Full Marks : +4 If **ONLY** the correct option is chosen;

Zero Marks : 0 in all other cases.

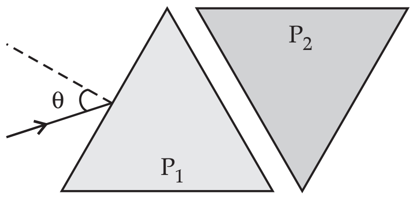
8. The dimensions of a cone are measured using a scale with a least count of 2 mm. The diameter of the base and the height are both measured to be 20.0 cm. The maximum percentage error in the determination of the volume is ....

9. A ball is thrown from the location $(x_0, y_0) = (0,0)$ of a horizontal playground with an initial speed v_0 at an angle θ_0 from the $+x$-direction. The ball is to be hit by a stone, which is thrown at the same time from the location $(x_1, y_1) = (L, 0)$. The stone is thrown at an angle $(180 - \theta_1)$ from the $+x$-direction with a suitable initial speed. For a fixed v_0, when $(\theta_0, \theta_1) = (45°, 45°)$, the stone hits the ball after time T_1, and when $(\theta_0, \theta_1) = (60°, 30°)$, it hits the ball after time T_2. In such a case, $\left(\frac{T_1}{T_2}\right)^2$ is ....

10. A charge is kept at the central point P of a cylindrical region. The two edges subtend a half-angle θ at P, as shown in the figure. When $\theta = 30°$, then the electric flux through the curved surface of the cylinder is ϕ. If $\theta = 60°$, then the electric flux through the curved surface becomes $\phi\sqrt{n}$ where the value of n is ....

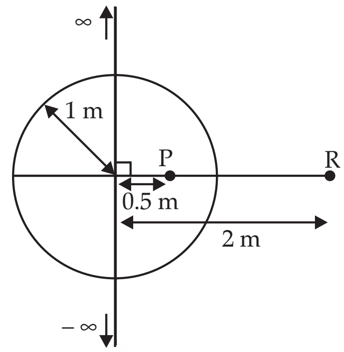


11. Two equilateral-triangular prisms P_1 and P_2 are kept with their sides parallel to each other, in vacuum, as shown in the figure. A light ray enters prism P_1 at an angle of incidence θ such that the outgoing ray undergoes minimum deviation in prism P_2. If the respective refractive indices of P_1 and P_2 are $\sqrt{\frac{3}{2}}$ and $\sqrt{3}$, then $\theta = \sin^{-1}\left[\sqrt{\frac{3}{2}}\sin\left(\frac{\pi}{\beta}\right)\right]$, where the value of β is ....



12. An infinitely long thin wire, having a uniform charge density per unit length of 5 nC/m, is passing through a spherical shell of radius 1 m, as shown in the figure. A 10 nC charge is distributed uniformly over the spherical shell. If the configuration of the charges remains static, the magnitude of the potential difference between points P and R, in Volt, is ....

[Given: In SI units $\frac{1}{4\pi\varepsilon_0} = 9 \times 10^9$, ln 2 = 0.7. Ignore the area pierced by the wire.]



13. A spherical soap bubble inside an air chamber at pressure $P_0 = 10^5$ Pa has a certain radius so that the excess pressure inside the bubble is $\Delta P = 144$ Pa. Now, the chamber pressure is reduced to $8P_0/27$ so that the bubble radius and its excess pressure change. In this process, all the temperatures remain unchanged. Assume air to be an ideal gas and the excess pressure ΔP in both the cases to be much smaller than the chamber pressure. The new excess pressure ΔP in Pa is ....

***General Instructions*:**

SECTION 4 (Maximum Marks : 12)

- This section contains **TWO (02)** paragraphs.
- Based on each paragraph, there are **TWO (02)** questions.
- The answer to each question is a **NUMERICAL VALUE**
- For each question, enter the correct numerical value of the answer using the mouse and the on-screen virtual numeric keypad in the place designated to enter the answer.
- If the numerical value has more than two decimal places, **truncate/round-off** the value to **TWO** decimal places.
- Answer to each question will be evaluated **according to the following marking scheme:**

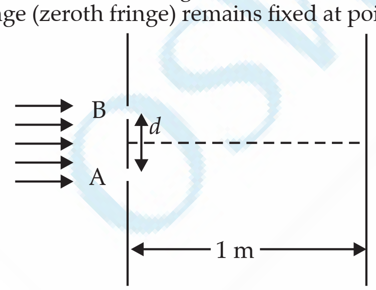
  Full Marks : +3 If ONLY the correct numerical value is entered in the designated place;

  Zero Marks : 0 in all other cases.

PARAGRAPH I

In a Young's double slit experiment, each of the two slits A and B, as shown in the figure, are oscillating about their fixed center and with a mean separation of 0.8 mm.

The distance between the slits at time t is given by $d = (0.8 + 0.04 \sin \omega t)$ mm, where $\omega = 0.08$ rad s^{-1}. The distance of the screen from the slits is 1 m and the wavelength of the light used to illuminate the slits is 6000 Å. The interference pattern on the screen changes with time, while the central bright fringe (zeroth fringe) remains fixed at point O.

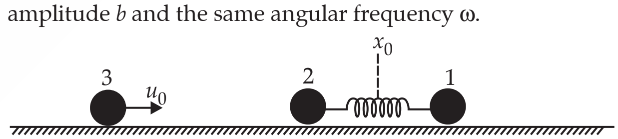


14. The 8th bright fringe above the point O oscillates with time between two extreme positions. The separation between these two extreme positions, in micrometer (μm), is ....

15. The maximum speed in μm/s at which the 8th bright fringe will move is ....

PARAGRAPH II

Two particles, 1 and 2, each of mass m, are connected by a massless spring, and are on a horizontal frictionless plane, as shown in the figure. Initially, the two particles, with their centre of mass at x_0, are oscillating with amplitude a and angular frequency ω. Thus, their positions at time t are given by $x_1(t) = (x_0 + d) + a \sin \omega t$ and $x_2(t) = (x_0 - d) - a \sin \omega t$, respectively, where $d > 2a$. Particle 3 of mass m moves towards this system with speed $u_0 = \frac{a\omega}{2}$ and undergoes instantaneous elastic collision with particle 2, at time t_0. Finally, particles 1 and 2 acquire a centre of mass speed v_{cm} and oscillate with amplitude b and the same angular frequency ω.



16. If the collision occurs at time $t_0 = 0$, the value of $v_{cm}/(a\omega)$ will be ....

17. If the collision occurs at time $t_0 = \frac{\pi}{2\omega}$, then the value of $\frac{4b^2}{a^2}$ will be ....

ANSWER KEY

Q.No.	Answer key	Topic's name	Chapter's name
1	A	Motional EMF, Inductance and Induced Electric Field	Electromagnetic Induction and Alternating Current
2	A	Acceleration due to gravity, Satellite and Kepler's Laws	Gravitation
3	A	X-Rays and Moseley's Law	Atomic Physics
4	A	Magnetic Force on Current Carrying Wires, Magnetic Moment	Magnetic Effect of Current and Magnetism
5	B, D	Electric Dipole, Behaviour of Conductors	Electrostatics and Capacitors
6	A, B, D	Surface Tension, Viscosity and Terminal Velocity	Fluids
7	A, B	Magnetic Force on Moving Charge in Uniform Fields	Magnetic Effect of Current and Magnetism
8	[3]	General Physics	General Physics
9	[2]	Motion in Straight Line, Motion in Plane	Kinematics
10	[3]	Electric Flux and Gauss Theorem	Electrostatics and Capacitors
11	[12]	Thin Lens and Combinations	Geometrical Optics
12	[171]	"Potential and Potential Energy, Work and Energy Conservation"	Electrostatics and Capacitors
13	[96]	Surface Tension, Viscosity and Terminal Velocity	Fluids
14	[598.00 to 602.00]	Interference, YDSE, Diffraction, Polarisation and Brewster's Law	Wave Optics
15	[23.50 to 24.50]	Interference, YDSE, Diffraction, Polarisation and Brewster's Law	Wave Optics
16	[0.74 to 0.76]	Miscellaneous Problems	Simple Harmonic Motion
17	[4.20 to 4.30]	Miscellaneous Problems	Simple Harmonic Motion

ANSWERS WITH EXPLANATIONS

1. Correct option is (A).

Induced emf $E = Bvl$

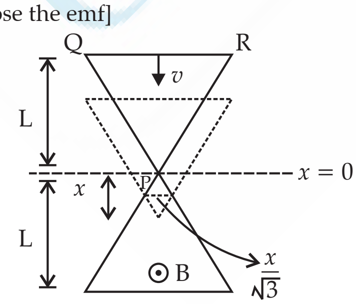
$$= Bv\frac{x}{\sqrt{3}}$$

i.e., $E \propto x$

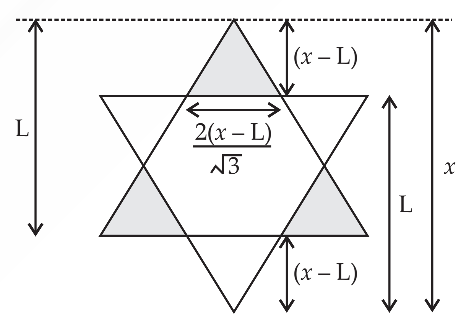
$$E = Bv\left[\frac{x}{\sqrt{3}} - \frac{2(x-L)}{\sqrt{3}} - \frac{2(x-L)}{\sqrt{3}}\right]$$

$$= \frac{Bv}{\sqrt{3}}(4L - 3x)$$

[considering the parts which will induce emf and which will oppose the emf]



At $x = \frac{4L}{3}$, $E = 0$



So, option (A) is correct.

2. Correct option is (A).

Time Period (T_0):

$$T_0^2 = \frac{4\pi^2}{GM}r_0^3$$

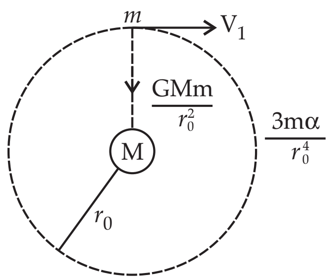
The additional force $f = \frac{d}{dr}V_c(r)$

$$= -\frac{3m\alpha}{r^4}$$

Now the net centripetal force

$$\frac{GMm}{r_0^2} - \frac{3m\alpha}{r_0^4} = \frac{mv_1^2}{r_0}$$

$$\Rightarrow \quad v_1 = \sqrt{\frac{GM}{r_0} - \frac{3\alpha}{r_0^3}}$$



Now, $$T_1 = \frac{2\pi r_0}{v_1}$$

$$\Rightarrow \quad T_1^2 = \frac{4\pi r_0^2}{\frac{GM}{r_0} - \frac{3\alpha}{r_0^3}}$$

$$\Rightarrow \quad T_1^2 = \frac{4\pi r_0^3}{GM\left[1 - \frac{3\alpha}{GMr_0^2}\right]}$$

We have to calculate,

$$\frac{T_1^2 - T_0^2}{T_1^2} = 1 - \left(\frac{T_0}{T_1}\right)^2$$

$$= 1 - \left(1 - \frac{3\alpha}{GMr_0^2}\right)$$

$$= \frac{3\alpha}{GMr_0^2}$$

3. **Correct option is (A).**

$$\frac{1}{\lambda_{k\alpha}} = R(Z-1)^2\left[1 - \frac{1}{4}\right]$$

$$\Rightarrow \quad \frac{1}{\lambda_{k\alpha}} = R(45)^2\frac{3}{4}$$

and $$\lambda_C = \frac{hc}{eV}$$

Now $$r = \frac{\lambda_{k\alpha}}{\lambda_C}$$

$$= \frac{4}{3R(45)^2} \times \frac{eV}{hc} = 2$$

$$\Rightarrow \quad \frac{eV}{hc} = \frac{2}{4} \times 3R(45)^2$$

So, $$r' = \frac{\lambda'_{k\alpha}}{\lambda_C}$$

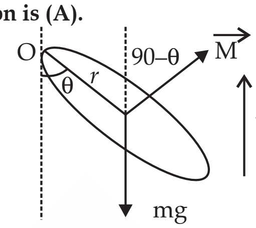
$$= \frac{4}{3R(40)^2} \times \frac{eV}{hc}$$

$$= \frac{4}{3R(40)^2} \times \frac{2}{4} \times 3R(45)^2$$

$$= \frac{2 \times (45)^2}{(40)^2}$$

$$= 2 \times \left(\frac{9}{8}\right)^2 = 2.53$$

4. **Correct option is (A).**



Let loop makes angle θ with vertical.

In equilibrium $\tau_{net} = 0$

$$\tau_0 = MB\sin(90 - \theta) - mg.\, r\sin\theta = 0$$

$$I.\pi r^2.B_0 \cos\theta = mgr.\sin\theta$$

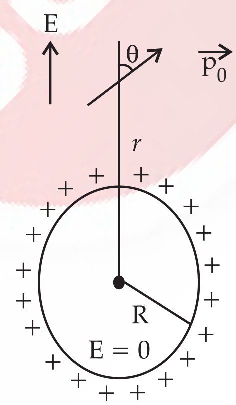
$$\tan\theta = \frac{\pi r I B_0}{mg}$$

5. **Correct options are (B, D).**

Electric field E acting on the dipole $= \frac{1}{4\pi\varepsilon_0}.\frac{q}{r^2}$

$$= \frac{1}{4\pi\varepsilon_0}.\frac{\sigma(4\pi R^2)}{r^2}$$

$$= \frac{\sigma R^2}{r^2\varepsilon_0}$$



The electric field inside the sphere is zero.

So, the dipole will oscillate when $r > R$.

Option (B) is correct.

Now, $$\omega = \sqrt{\frac{PE}{I}} = \sqrt{\frac{p_0\sigma R^2}{Ir^2\varepsilon_0}}$$

when $r = 2R$, then $\omega = \sqrt{\frac{p_0\sigma}{4I\varepsilon_0}}$

Option (C) is incorrect.

when $r = 10R$, then $\omega = \sqrt{\frac{p_0\sigma}{100I\varepsilon_0}}$

Option (D) is correct.

6. **Correct options are (A, B, D).**

Given, $$R = \frac{3}{2} \times 10^{-2}\ \text{m}$$

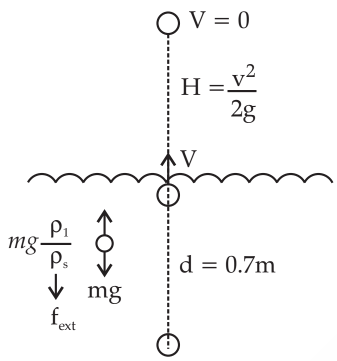
$$m = \frac{22}{7} \times 10^{-3} \text{ kg}$$

⇒ Density of the ball

$$\rho_S = \frac{m}{\frac{4}{3}\pi R^3}$$

$$= \frac{\frac{22}{7}\times 10^{-3}}{\frac{4}{3}\times\frac{22}{7}\times\left(\frac{3}{2}\times 10^{-2}\right)^3}$$

$$\rho_S = \frac{2}{9}\times 10^3 \text{ kgm}^{-3}$$



Now, $$F_{\text{ext}} = mg\frac{\rho_l}{\rho_S} - mg$$

$$= mg\left[\frac{\rho_l}{\rho_S} - 1\right]$$

$$= \frac{22}{7}\times 10^{-3}\times 10\times\left[\frac{10^3}{\frac{2}{9}\times 10^3} - 1\right]$$

$$= \frac{22}{7}\times 10^{-2}\times\left(\frac{9}{2} - 1\right)$$

$$= 0.11 \text{ N}$$

For option (A), $W = Fd$

$= 0.11 \times 0.7 = 0.077$ J (correct)

For option (B), $$0.077 = \frac{1}{2}mv^2$$

⇒ $$v^2 = \frac{0.077\times 2}{m} = \frac{0.077\times 2}{\frac{22}{7}\times 10^{-3}}$$

⇒ $$v = \sqrt{49} = 7 \text{ ms}^{-1}$$ (correct)

For option (C), $$H = \frac{v^2}{2g} = \frac{49}{20}$$

$= 2.45$ m (incorrect)

For option (D),

Maximum viscous force $F_{V_{\max}} = 6\pi\eta Rv$

$$= 6\times\frac{22}{7}\times 10^{-3}\times\frac{3}{2}\times 10^{-2}\times 7$$

$$= 9 \times 22 \times 10^{-5} \text{ N}$$

Now, $$\frac{F_{\text{net}}}{Fv_{\max}} = \frac{500}{9}$$

7. Correct options are (A, B).

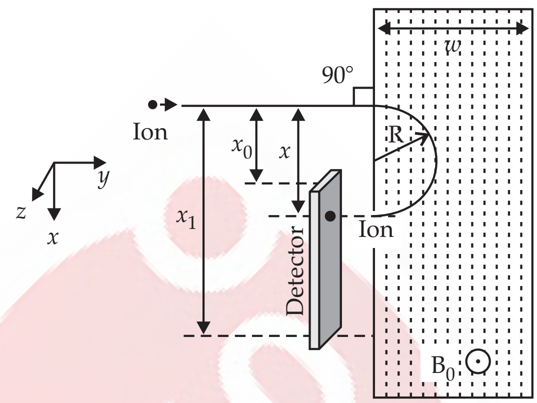
KE of the ion $= 192$eV

$$R = \frac{mv}{qB} = \frac{\sqrt{2meV}}{eB}$$

$$x = 2R$$

$$= 2\times\frac{\sqrt{2meV}}{eB}$$

$$= 2\times\sqrt{\frac{2mV}{eB^2}}$$



For option (A), $$x = 2\times\sqrt{\frac{2\times\frac{5}{3}\times 10^{-27}\times 192}{1.6\times 10^{-19}\times 10^{-2}}}$$

$= 2 \times 2 \times 10^{-2}$

$= 0.04$ m

$= 4$ cm (correct)

For option (B), $$x = 2\times\sqrt{\frac{2\times 144\times\frac{5}{3}\times 10^{-27}\times 192}{1.6\times 10^{-19}\times 10^{-2}}}$$

$= 2 \times 2 \times 12 \times 10^{-2}$

$= 48$ cm (correct)

For option (C),

When $A_m = 1, x_0 = 4$ cm

and when $A_m = 196, x_1 = 56$ cm

So $x_1 - x_0 = 52$ cm (incorrect)

For option (D), $$x = 2\times\sqrt{\frac{2\times 196\times\frac{5}{3}\times 10^{-27}\times 192}{1.6\times 10^{-19}\times 10^{-2}}}$$

$= 56$ cm

for $A_m = 196$,

$$R = \frac{x}{2} = 28 \text{ cm}$$ (incorrect)

8. Correct answer is [3].

Volume $$V = \frac{1}{3}\pi\left(\frac{D}{2}\right)^2 H$$

∴ % Error in $V = 2$(% error in D) + % error in H.

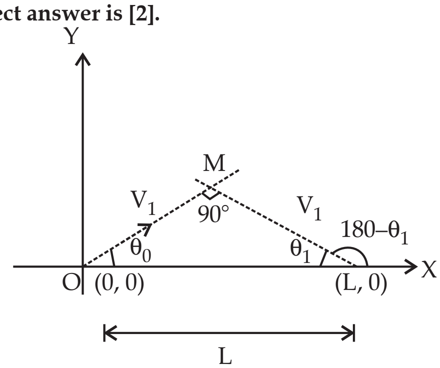
∵ Least count is 2 mm.

∴ $$\text{\% error in } D = \frac{0.2}{20}\times 100\% = 1\%$$

and $$\text{\% error in } H = \frac{0.2}{20}\times 100\% = 1\%$$

So, % error in $V = 2 \times 1\% + 1\% = 3\%$

9. Correct answer is [2].



Here relative acceleration = 0

$$OM = L\cos 45° = \frac{L}{\sqrt{2}} \quad (\text{case}-1)$$

and $$OM = L\cos 60° = \frac{L}{2} \quad (\text{case}-2)$$

Now, $$T_1 = \frac{\frac{L}{\sqrt{2}}}{v_0} \text{ and } T_2 = \frac{\frac{L}{2}}{v_0}$$

$$\Rightarrow \quad \left(\frac{T_1}{T_2}\right)^2 = \left(\frac{2}{\sqrt{2}}\right)^2 = 2$$

10. Correct answer is [3].

Flux through the curved surface = total flux – flux through the solid angles

Now, $$\phi = \frac{q}{\varepsilon_0} - 2\times\frac{\frac{q}{\varepsilon_0}}{4\pi}\times 2\pi(1-\cos 30°)$$

$$= \frac{q}{\varepsilon_0} - \frac{q}{\varepsilon_0}\left(1-\frac{\sqrt{3}}{2}\right)$$

$$= \frac{\sqrt{3}q}{2\varepsilon_0}$$

and $$\frac{\phi}{\sqrt{n}} = \frac{q}{\varepsilon_0} - 2\times\frac{\frac{q}{\varepsilon_0}}{4\pi}\times 2\pi(1-\cos 60°)$$

$$= \frac{q}{\varepsilon_0} - \frac{q}{\varepsilon_0}\left(1-\frac{1}{2}\right)$$

$$= \frac{q}{\varepsilon_0} - \frac{q}{2\varepsilon_0}$$

$$= \frac{q}{2\varepsilon_0}$$

So, $$\frac{\phi}{\frac{\phi}{\sqrt{n}}} = \frac{\sqrt{3}q}{2\varepsilon_0}\times\frac{2\varepsilon_0}{q} = \sqrt{3}$$

$$\Rightarrow \quad \sqrt{n} = \sqrt{3}$$

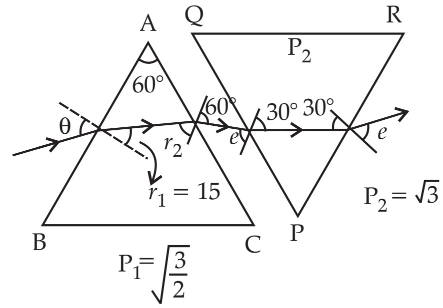
So, $$n = 3$$

11. Correct answer is [12].

For the face PQ in the second prism, applying Snell's law

$$\sqrt{3}\sin 30° = \sin e$$

$$\Rightarrow \quad e = 60°$$



Again, applying Snell's law at the face AC in the first prism,

$$\sqrt{\frac{3}{2}}\sin r_2 = \sin 60°$$

$$\Rightarrow \quad \sqrt{\frac{3}{2}}\sin r_2 = \frac{\sqrt{3}}{2}$$

$$\Rightarrow \quad \sin r_2 = \frac{\sqrt{3}}{2}\times\sqrt{\frac{2}{3}} = \frac{1}{\sqrt{2}}$$

$$\Rightarrow \quad r_2 = 45°$$

So, $$r_1 = 60 - 45 = 15°$$

Applying Snell's law at the face AB of the first prism,

$$\sin\theta = \sqrt{\frac{3}{2}}(\sin 15°)$$

$$\Rightarrow \quad \sin\theta = \sqrt{\frac{3}{2}}\sin\left(\frac{\pi}{12}\right)$$

$$\Rightarrow \quad \beta = 12$$

12. Correct answer is [171].

Given, $\lambda = 5\times10^{-9}$ C/m

$R = 1$ m

$Q = 10\times10^{-9}$ C $= 10^{-8}$ C

Electrostatics Potential Due to shell,

$$V_P = \frac{KQ}{R} = \frac{9\times10^9\times10^{-8}}{1} = 90 \text{ V}$$

$$V_R = \frac{KQ}{R} = \frac{9\times10^9\times10^{-8}}{2} = 45 \text{ V}$$

$$V_P - V_R = 90 - 45 = 45 \text{ V}$$

Due to line charge,

$$VP - VR = V_{PR}$$

$$= \int_{0.5}^{2}\frac{2K\lambda}{x}dx$$

$$= 2K\lambda\ln(4)$$

$$= 2\times9\times10^9\times5\times10^{-9}\times2\times\frac{7}{10}$$

$$= 126 \text{ V}$$

So, the total potential difference

$$V_{PR} = 126 + 45 = 171 \text{ V}$$

13. Correct answer is [96].

Case - 1

$$P - P_0 = \Delta P = \frac{4T}{R}$$

$$P = \left(P_0 + \frac{4T}{R}\right)$$

Case - 2

$$P_1 - \frac{8P_0}{27} = \Delta P_1 = \frac{4T}{R_1}$$

$$P_1 = \frac{4T}{R_1} + \frac{8P_0}{27}$$

As this is a constant temperature process,

So, $PV = P_1V_1$

$$\left(P_0 + \frac{4T}{R}\right)\frac{4}{3}\pi R^3 = \left(\frac{4T}{R_1} + \frac{8P_0}{27}\right)\frac{4}{3}\pi R_1^3$$

Neglecting the terms $\frac{4T}{R}$ and $\frac{4T}{R_1}$

$$R = \frac{2}{3}R_1$$

$$\Rightarrow \quad R_1 = \frac{3}{2}R$$

$$\Delta P_1 = \frac{4T}{R_1} = \frac{4T}{3R} \times 2$$

$$= \frac{2}{3} \times (144) = 96 \text{ Pa}$$

14. Correct answer is [601.5].

Given,
$d = 0.8 \times 10^{-3}$ m
$d = 0.8 + 0.04 \sin\omega t$ (at time t)
$\omega = 0.08$ rad/s
$D = 1$ m
$\lambda = 6000\text{Å} = 6 \times 10^{-7}$ m
$d_{max} = 0.8 + 0.04$ mm
$d_{min} = 0.8 - 0.04$ mm

$$y = 8\frac{\lambda D}{d}$$

So, $$y_{max} = 8\frac{\lambda D}{d_{min}}$$

$$\Rightarrow \quad y_{min} = 8\frac{\lambda D}{d_{max}}$$

$$\Rightarrow \quad y_{max} - y_{min} = 8\lambda D\left[\frac{1}{d_{min}} - \frac{1}{d_{max}}\right]$$

$$= 8 \times 6 \times 10^{-7} \times 1\left[\frac{1}{0.8 - 0.04} - \frac{1}{0.8 + 0.04}\right] \times 10^3$$

$$= 8 \times 6 \times 10^{-4} \times 1\left[\frac{2 \times 0.04}{(0.8)^2 - (0.04)^2}\right]$$

$$= 601.5\ \mu\text{m}$$

15. Correct answer is [24].

Distance of 8th bright fringe from the point O

$$y = \frac{n\lambda D}{d}$$

$$v_{8thB} = \frac{dy}{dt} = -\frac{n\lambda D}{d^2} \times \frac{d(d)}{dt}$$

$$= \frac{8 \times 6 \times 10^{-7} \times 1}{(0.8 \times 10^{-3})^2} \times 0.04 \times 0.08 \times 10^{-3}$$

$$= 24\ \mu\text{m/s}$$

16. Correct answer is [0.75].

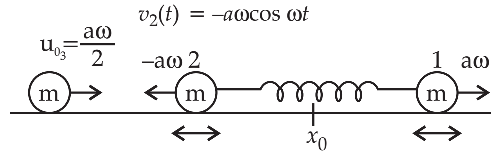
Position of particle (1)

$$x_1(t) = (x_0 + d) + a\sin\omega t$$

and position of particle (2)

$$x_2(t) = (x_0 - d) - a\sin\omega t$$

$$\Rightarrow \quad v_2(t) = -a\omega\cos\omega t$$



at $t = 0, v_2(t) = -a\omega$ (towards left)

and $v_1(t) = a\omega$ (towards right)

After collision, $$v_{cm} = \frac{m(a\omega) + m\left(\frac{a\omega}{2}\right)}{2m}$$

$$= \frac{3}{4}a\omega$$

Now $$\frac{v_{cm}}{a\omega} = \frac{3}{4} = 0.75$$

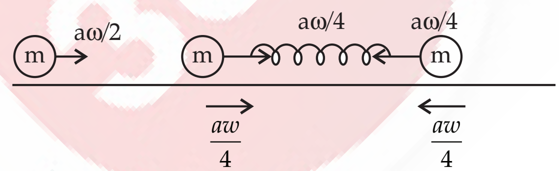
17. Correct answer is [4.25].

At $$t_0 = \frac{\pi}{2\omega} = \frac{T}{4},$$

Particles are at extreme positions.

So, the velocities of (1) and (2) = 0

$$v_{cm} = \frac{m\left(\frac{a\omega}{2}\right) + m(0)}{2m} = \frac{a\omega}{4}$$



This is the velocity of com after collision with particle (2). In frame of com, applying the law of conservation of energy,

$$\frac{1}{2}m\left(\frac{a\omega}{4}\right)^2 \times 2 + \frac{1}{2}k(2a)^2 = \frac{1}{2}k(2b)^2$$

We have to use, $$\frac{1}{2}k(2a)^2 = \frac{1}{2} \times m(a\omega)^2 \times 2$$

So, $$\frac{m}{16}(a\omega)^2 + \frac{1}{2}k(2a)^2 = \frac{1}{2}k(2b)^2$$

$$\Rightarrow \quad \frac{1}{16}(2ka^2) + 2ka^2 = 2kb^2$$

$$\Rightarrow \quad \frac{17}{16}a^2 = b^2$$

$$\Rightarrow \quad \frac{b^2}{a^2} = \frac{17}{16}$$

So, $$\frac{4b^2}{a^2} = \frac{17}{4} = 4.25$$

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